



# Cosmological Mysteries

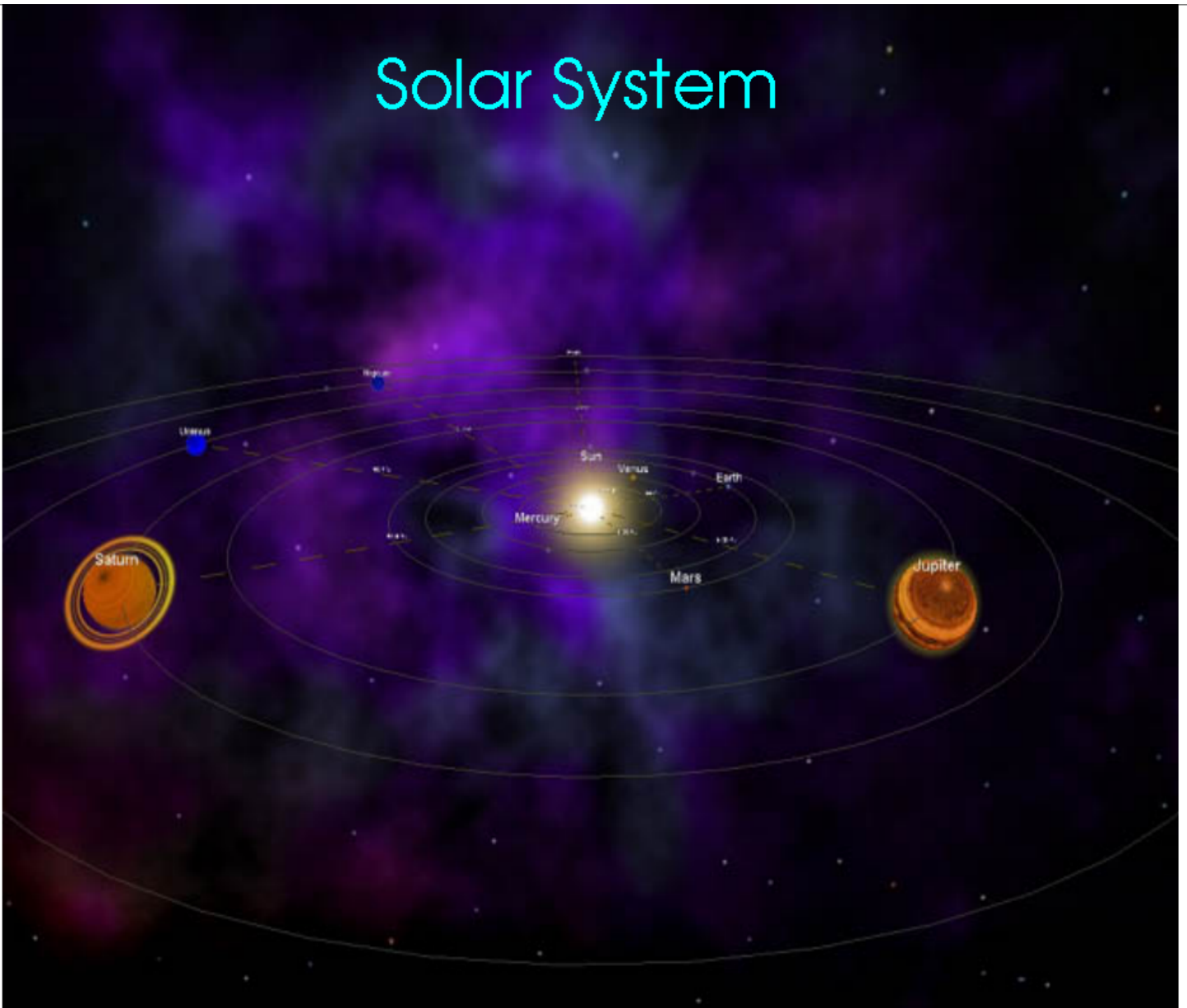
*Dark Matter  
and  
Structure formation in the Universe*

Andrey Kravtsov

*Kavli Institute for Cosmological Physics  
Department of Astronomy & Astrophysics  
University of Chicago*

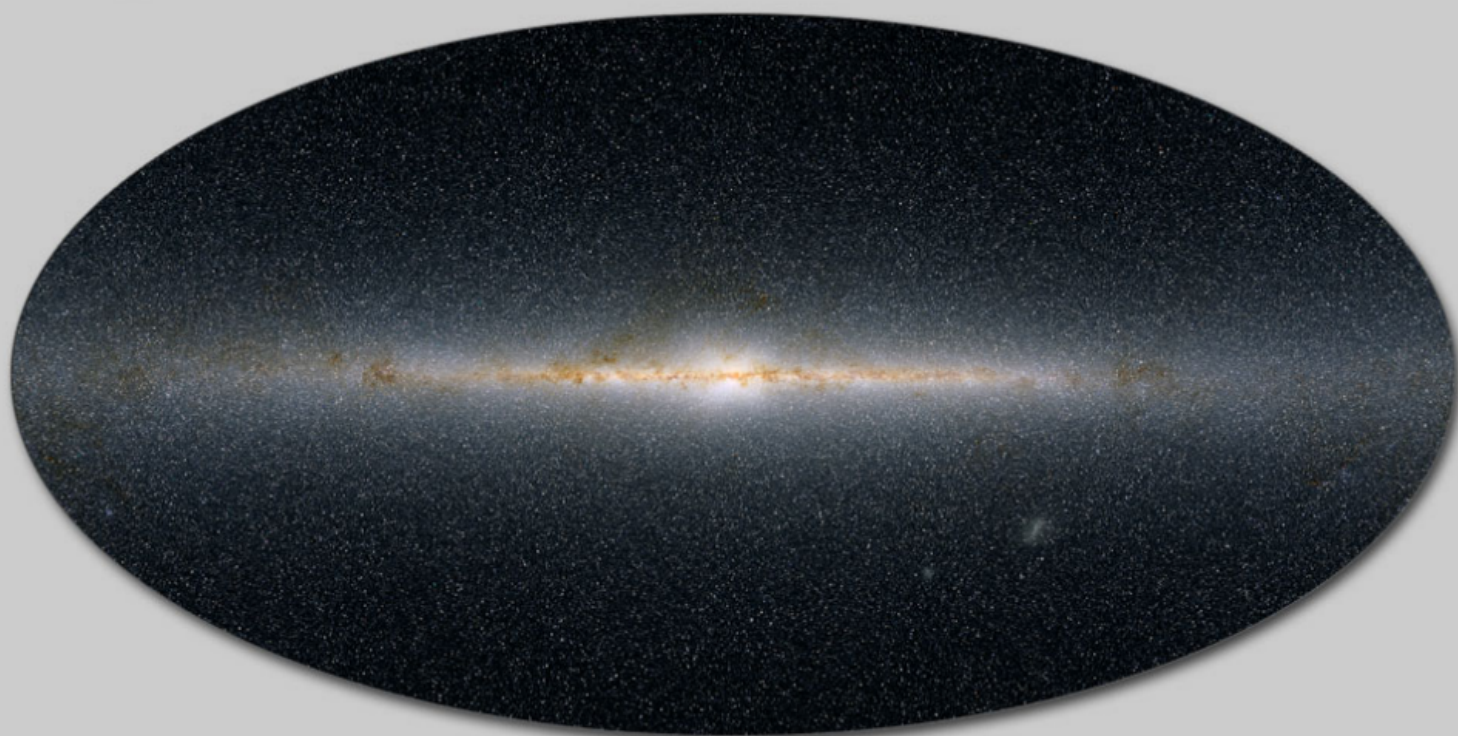
<http://astro.uchicago.edu/~andrey/talks/mysteries>

# Solar System



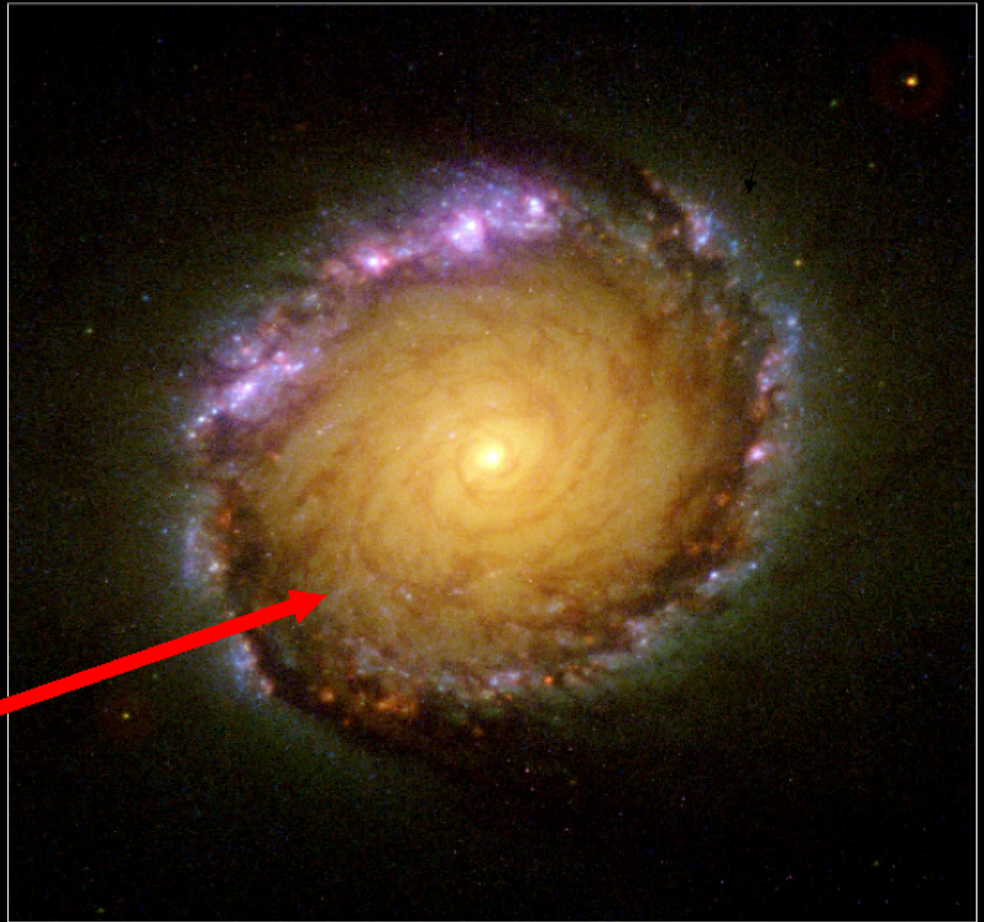
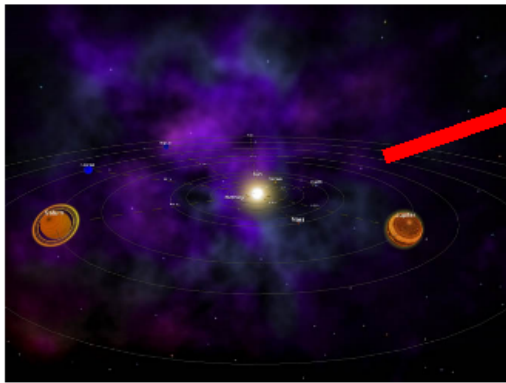


**2MASS** *showcase*



**The Infrared Milky Way** This map of the infrared sky includes the light of a half billion stars

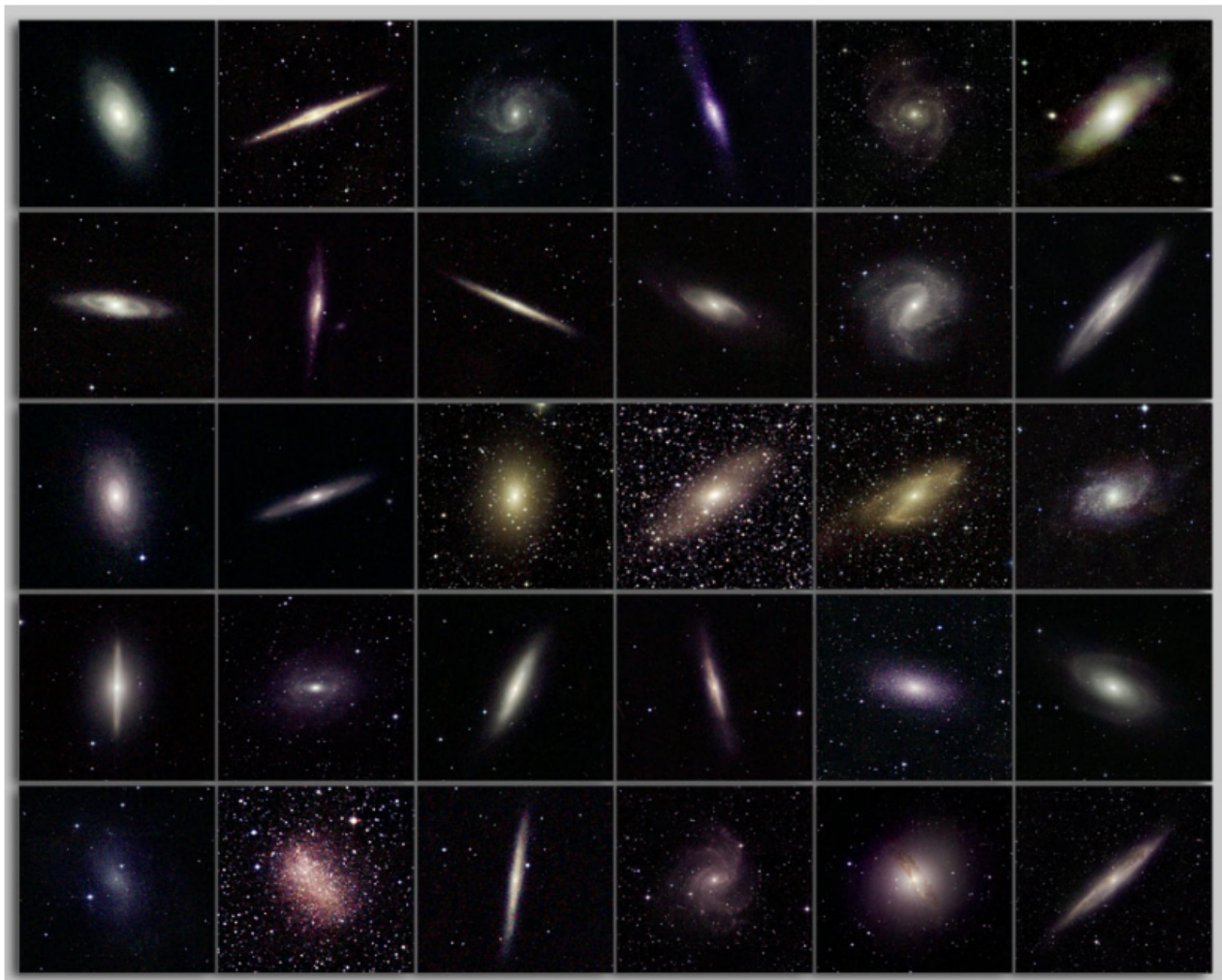
Two Micron All Sky Survey Image Mosaic: Infrared Processing and Analysis Center/Caltech & University of Massachusetts



**Galaxy NGC 1512**  
**Hubble Space Telescope • FOC • NICMOS • WFPC2**

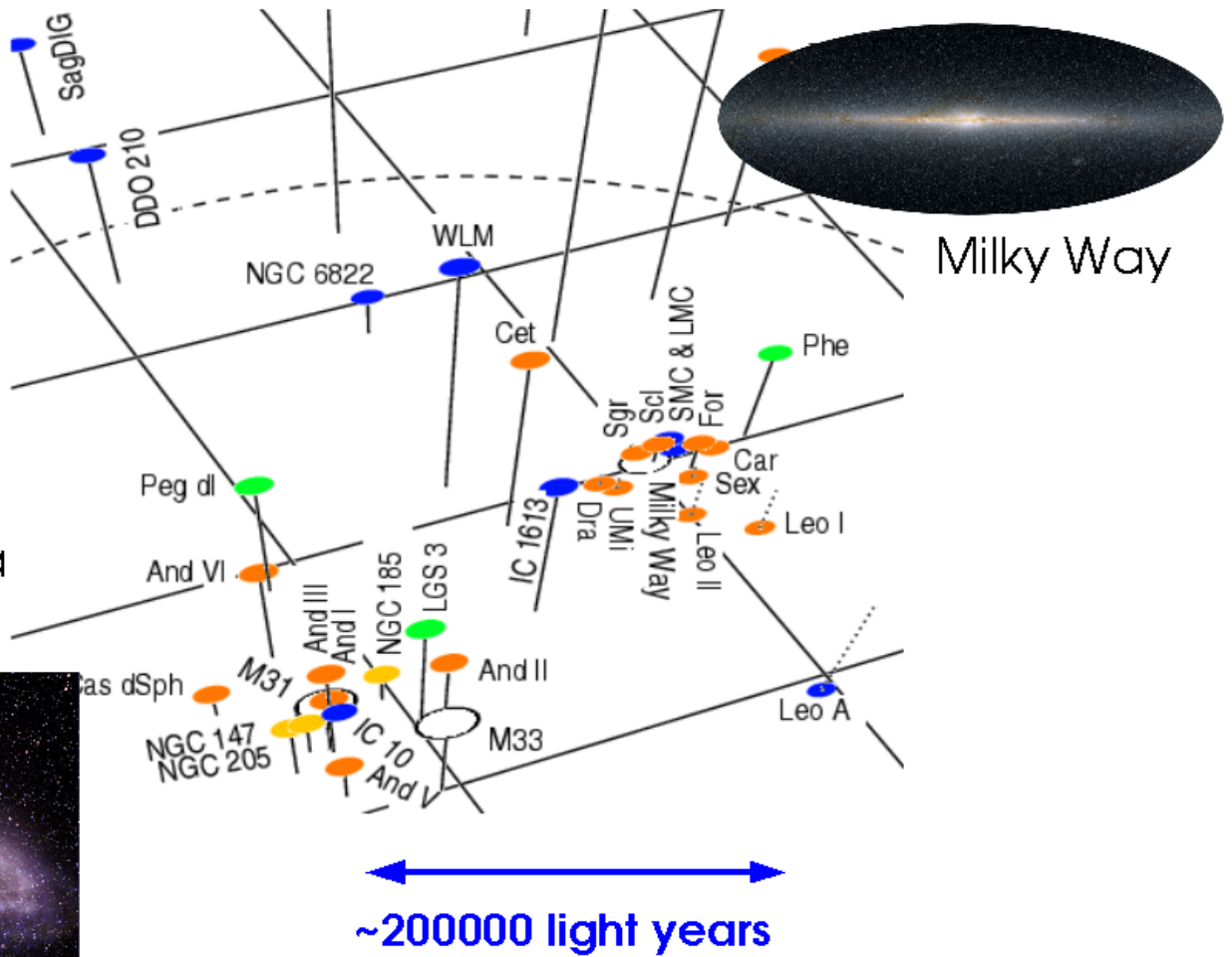
NASA, ESA, and D. Maoz (Tel-Aviv University and Columbia University) • STScI-PRC01-16

## Galaxies come in different shapes and sizes



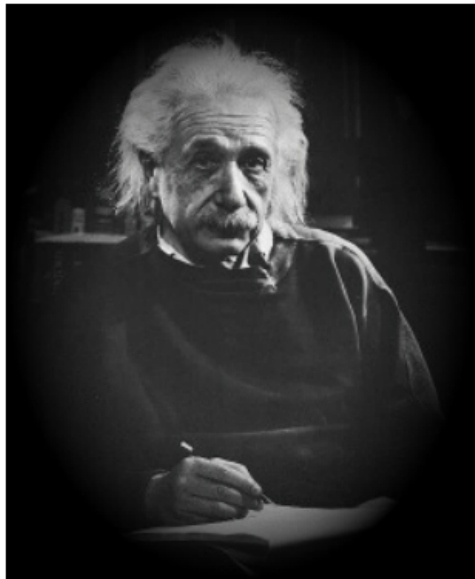
# The Local Group

- dlrr
- dlrr/dSph
- dEs
- dSph



Andromeda galaxy

## Einstein's Cosmological Principle:

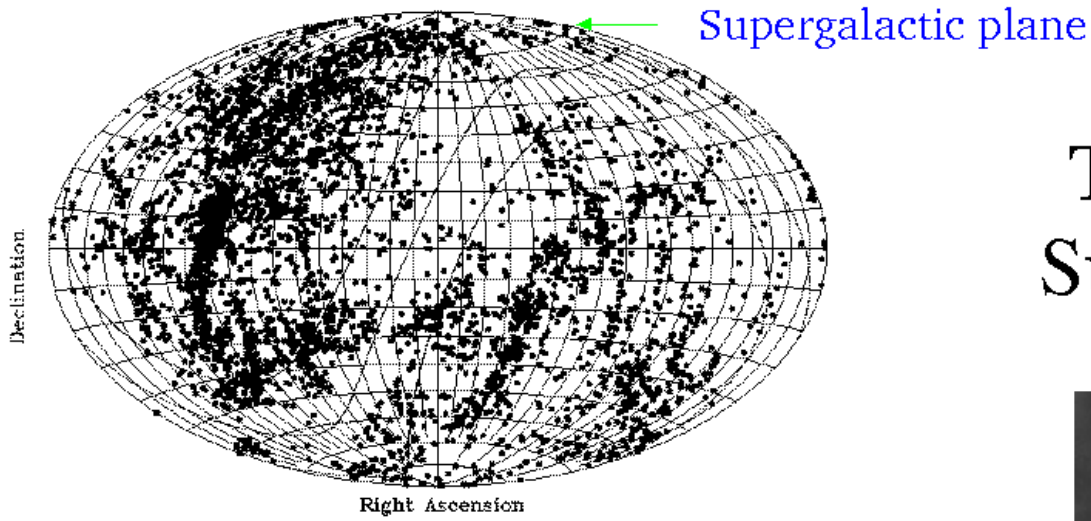


Albert Einstein  
(1878- 1955)

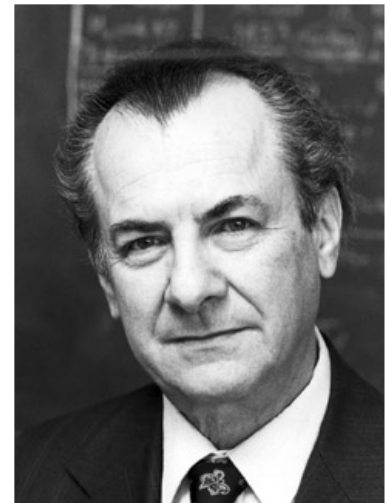
The Universe, on average, is  
homogeneous (equal density  
everywhere if averaged over a  
sufficiently large volume) and  
isotropic (it looks the same in all  
directions)

***Is distribution of galaxies  
in space  
consistent with this?***



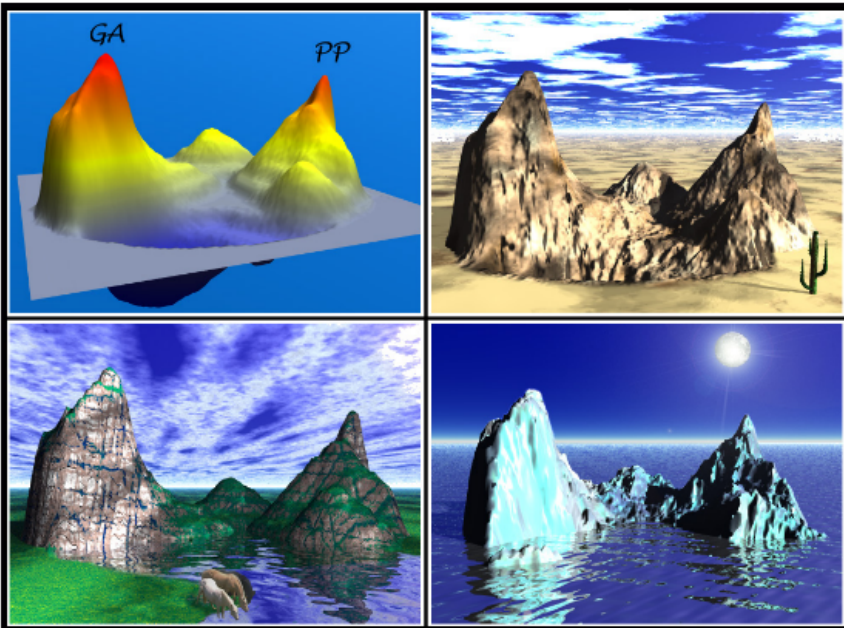


# The Local Supercluster

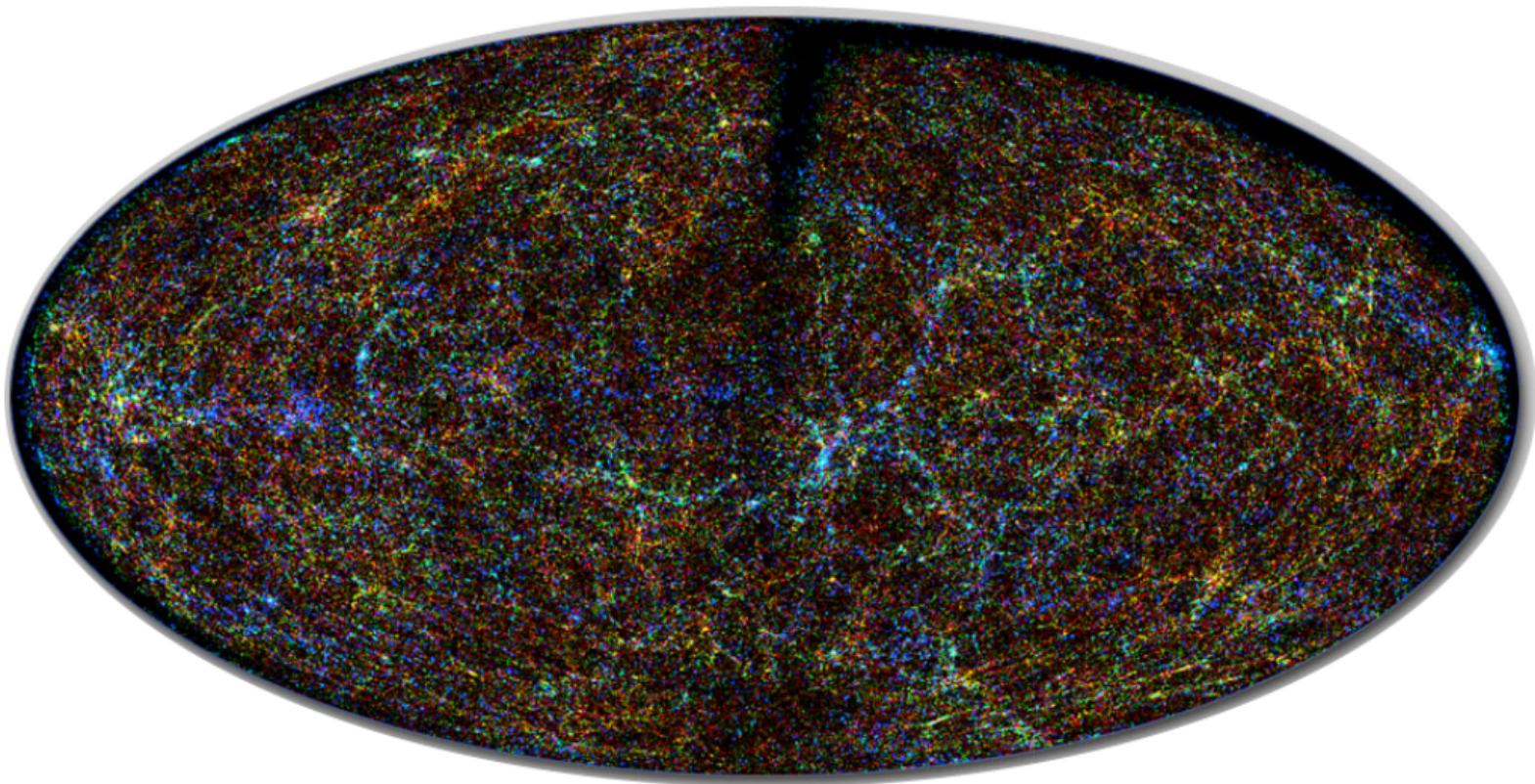


Gerard de Vaucouleurs  
1918- 1995

G. de Vaucouleurs



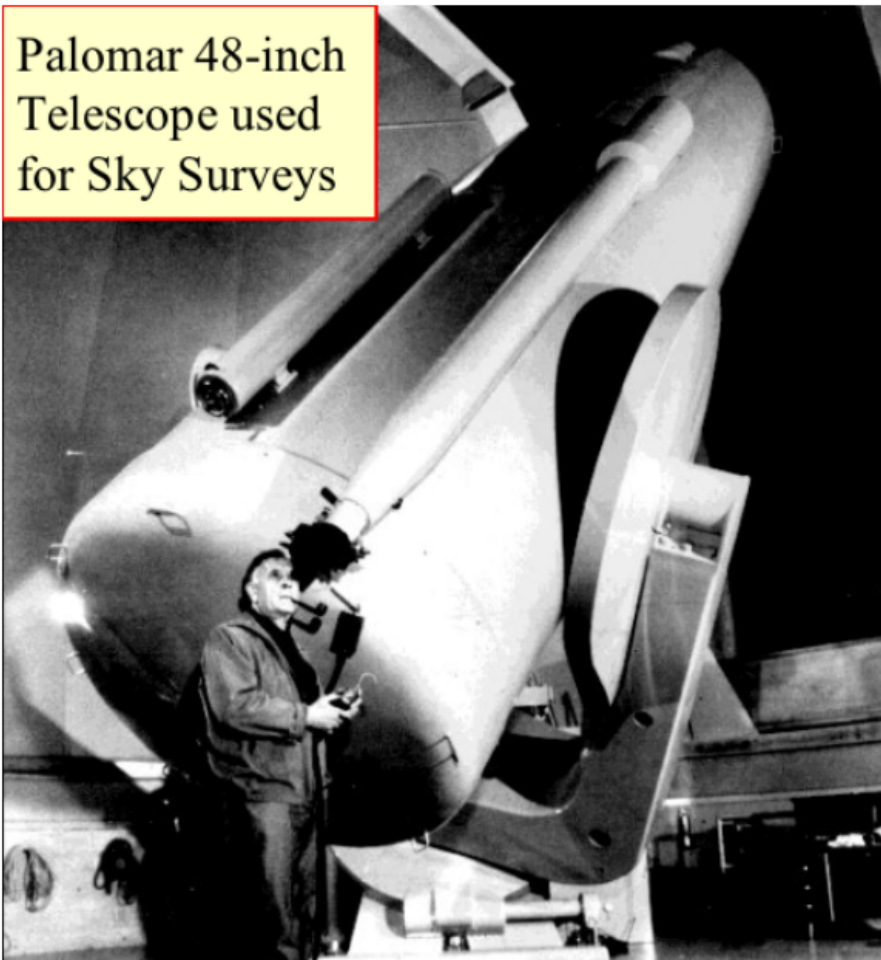
# Sky Distribution of Galaxies



## From 2D to 3D:

*using expansion of the Universe to map it*

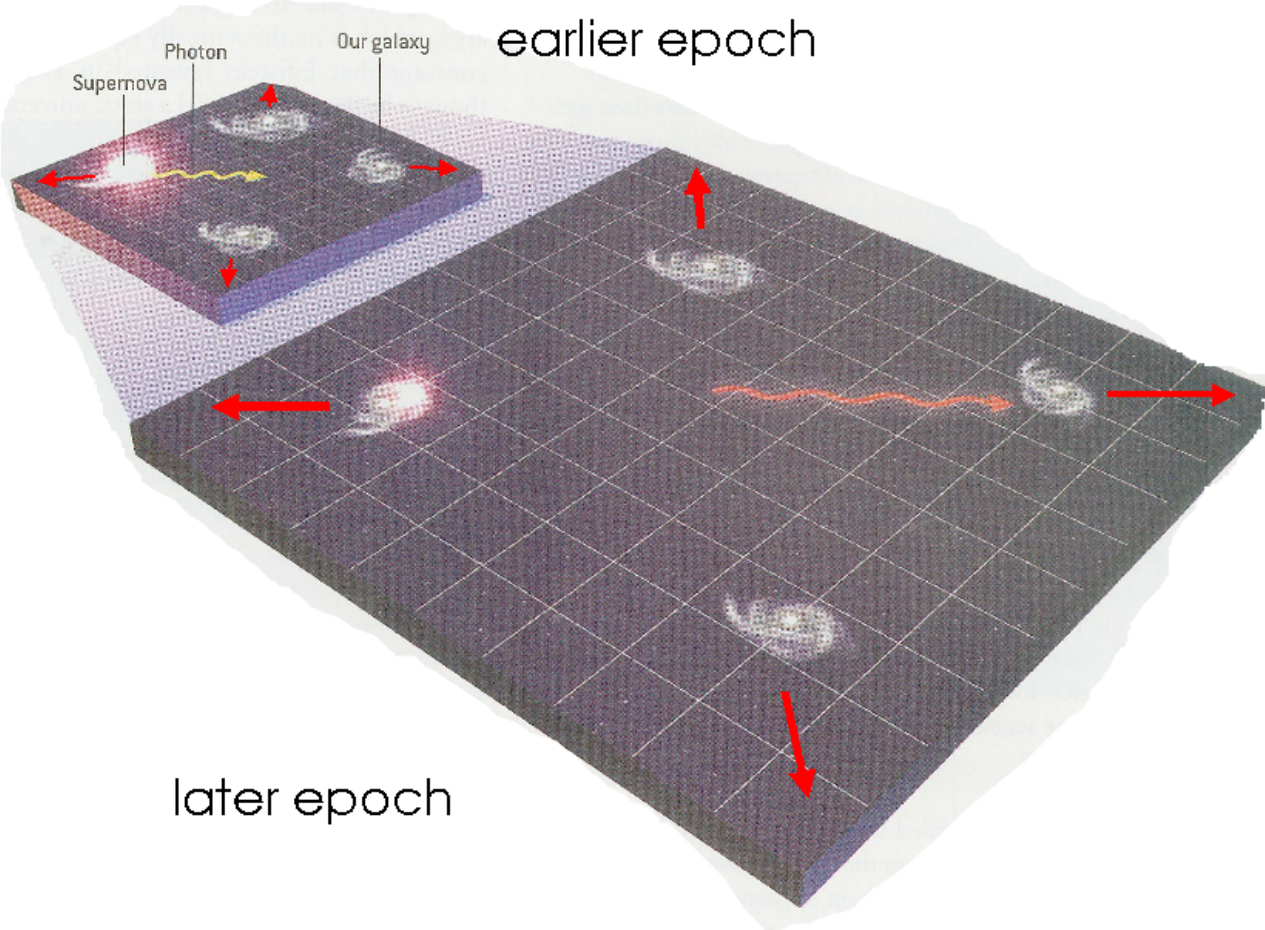
Palomar 48-inch  
Telescope used  
for Sky Surveys



**Edwin Hubble**  
(1889- 1953)

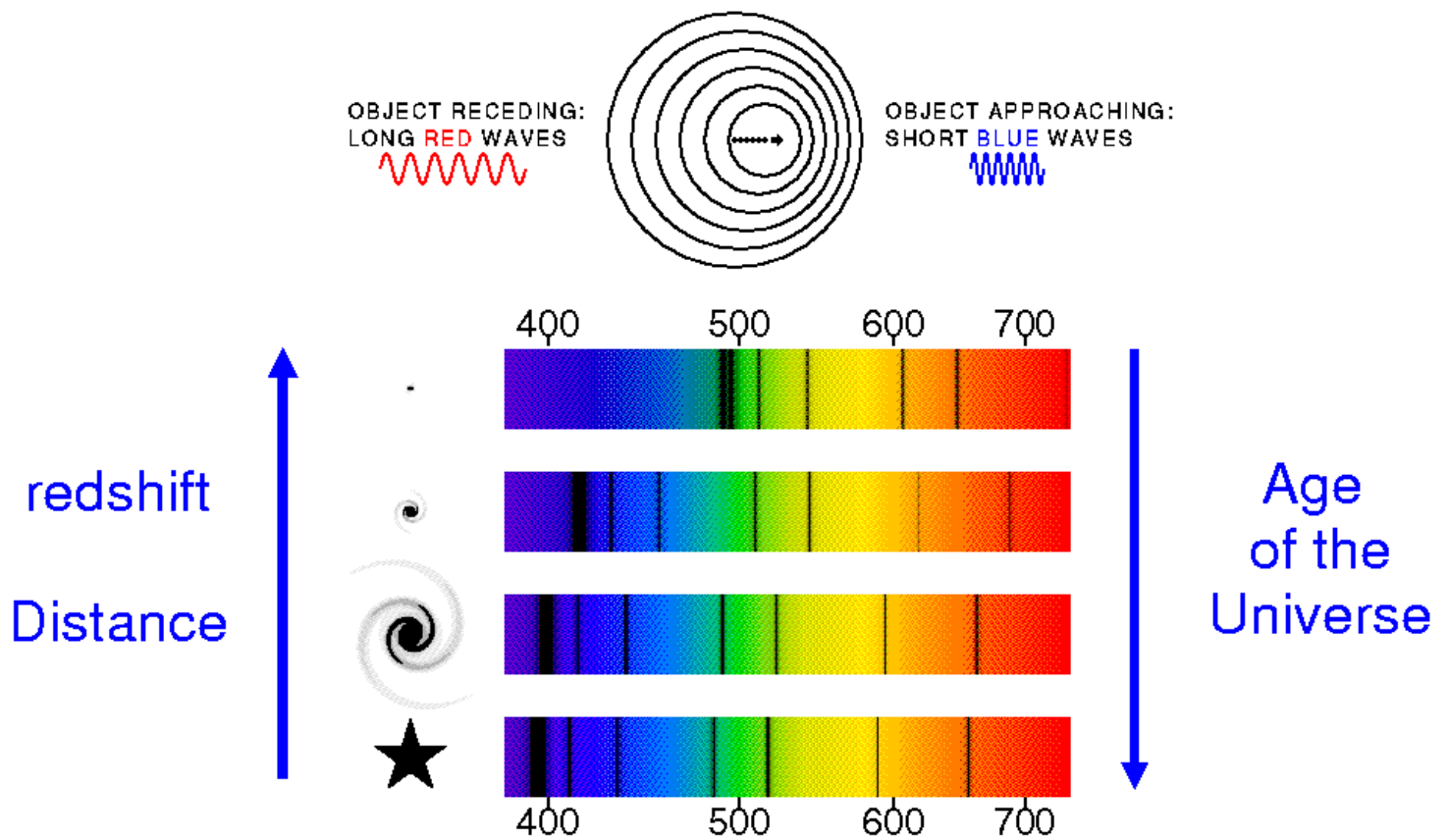
U.Chicago alum!  
(PhD, 1917)

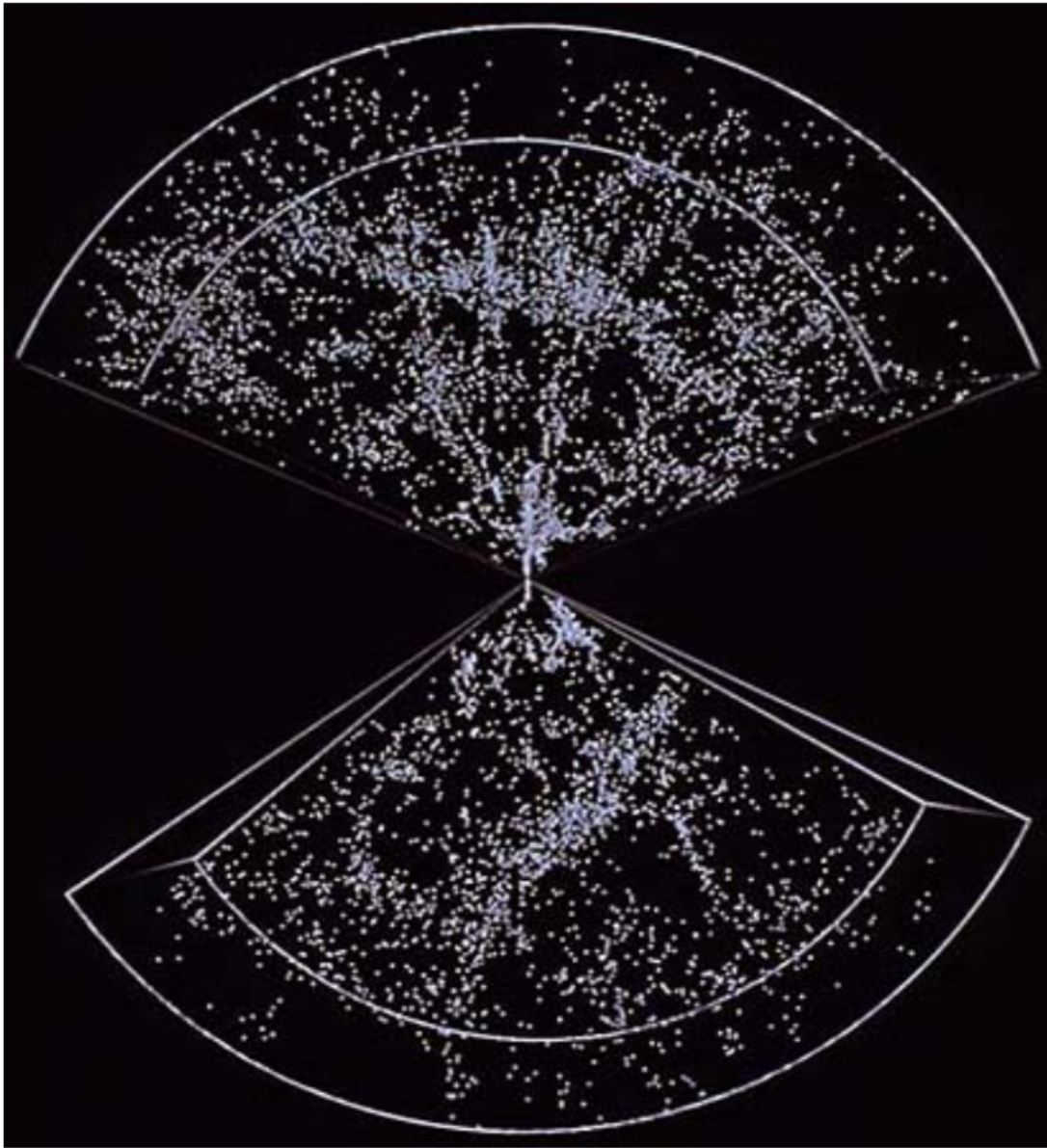
# *Expansion of space*



later epoch

# Cosmological Redshift as a measure of distance and time



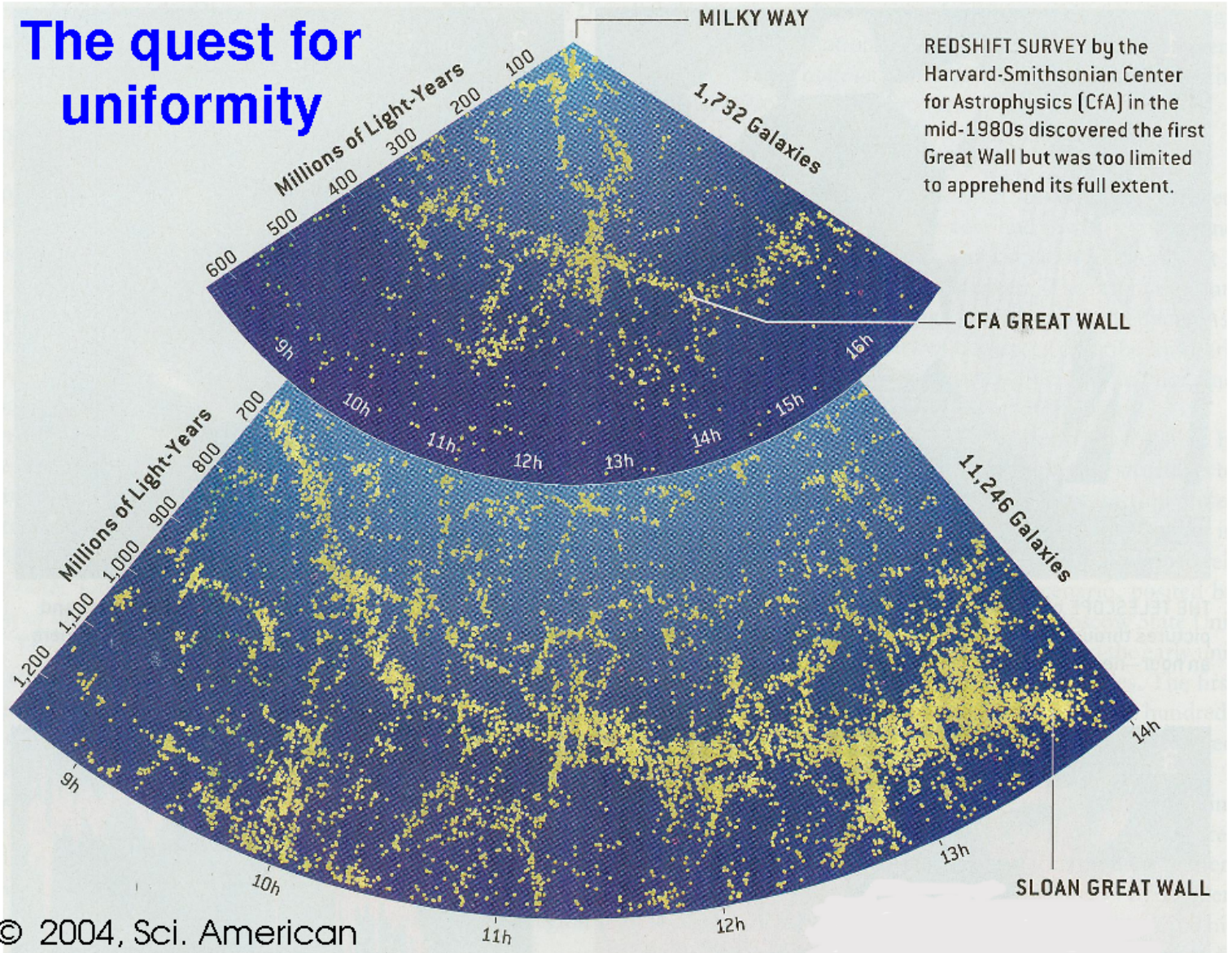


## Large- scale distribution of galaxies

at distances  
less than  
300 million  
light years

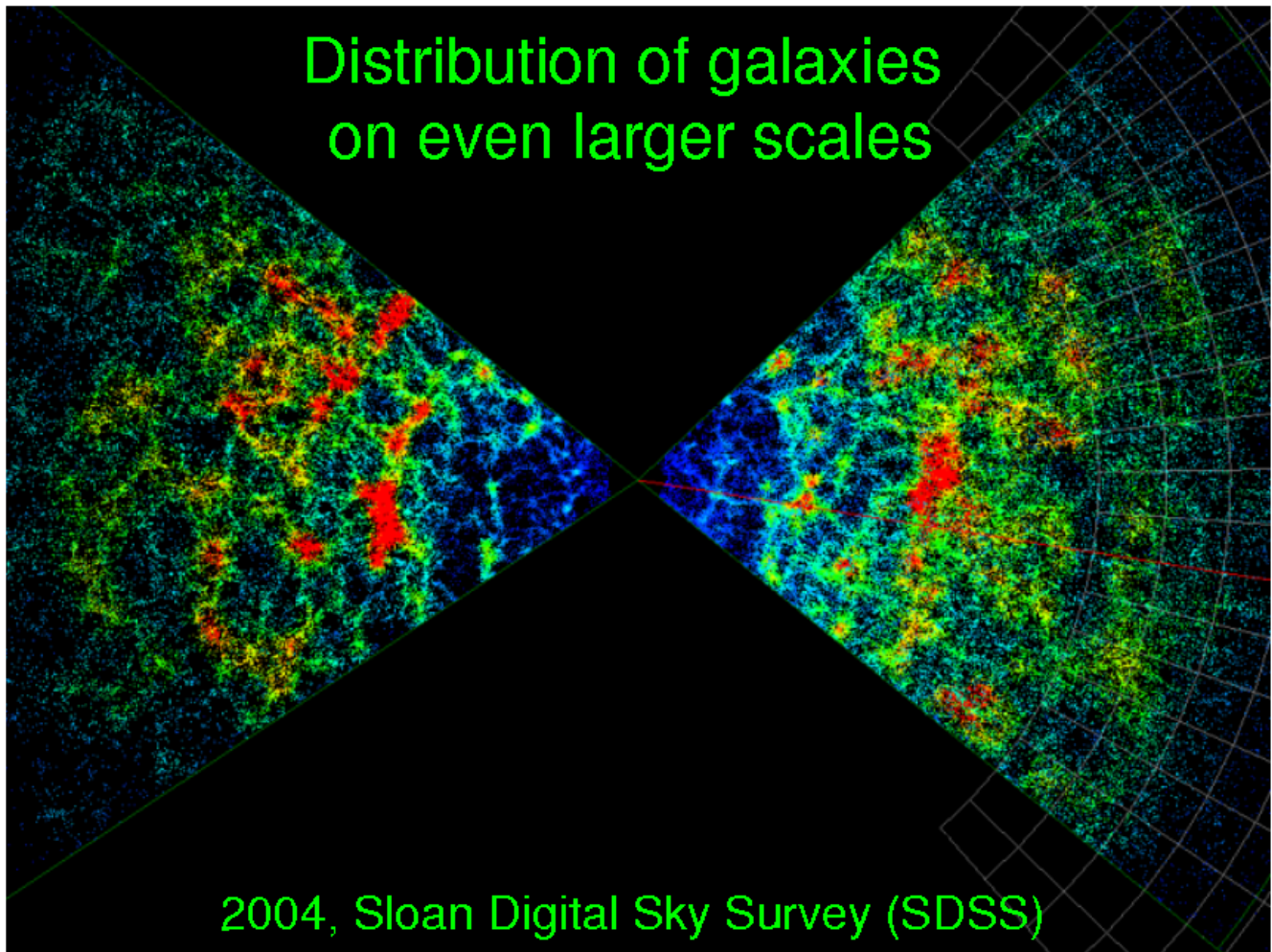
CfA galaxy  
survey  
1980- 1990

# The quest for uniformity



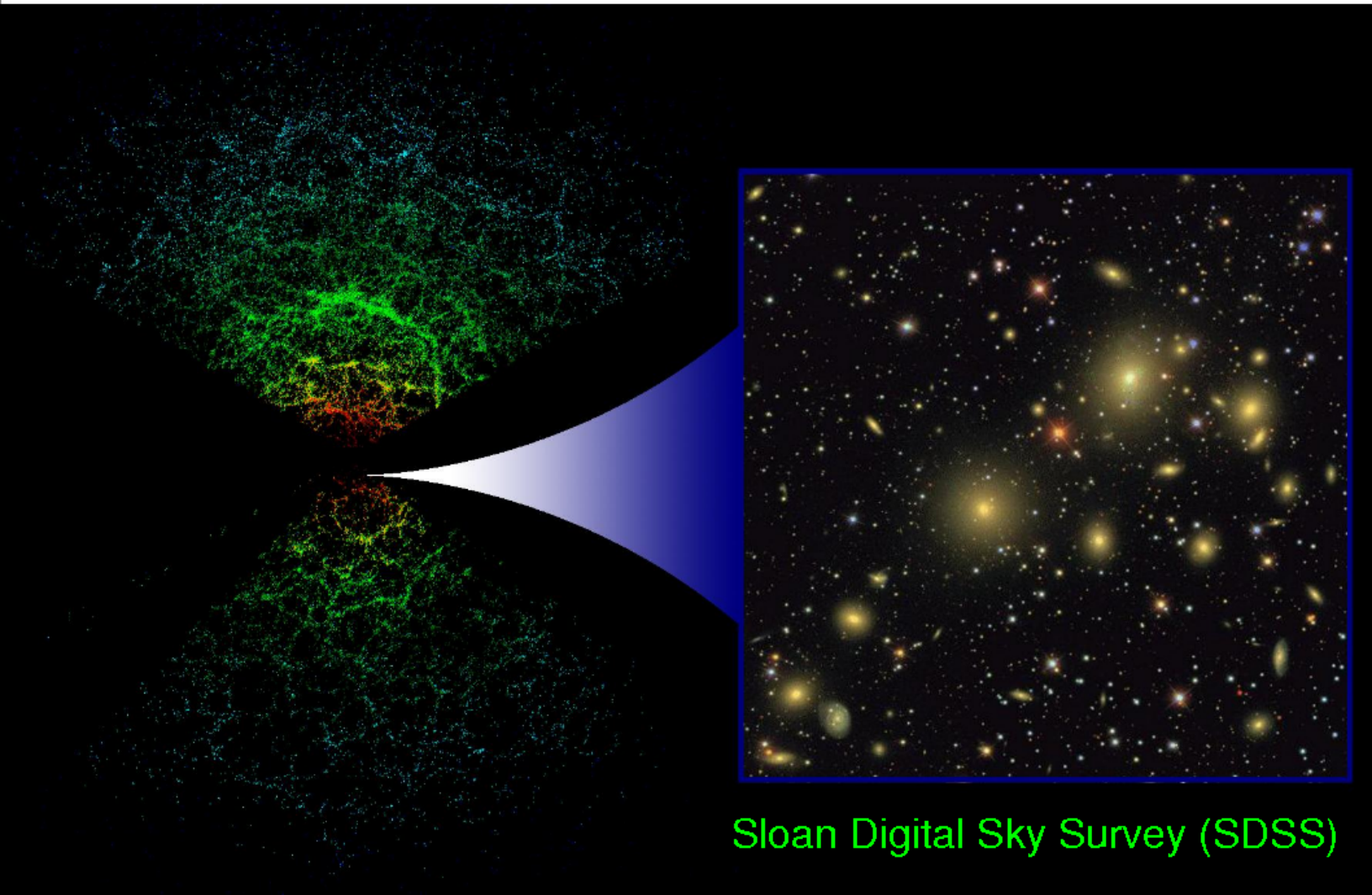
REDSHIFT SURVEY by the Harvard-Smithsonian Center for Astrophysics (CfA) in the mid-1980s discovered the first Great Wall but was too limited to apprehend its full extent.

## The end of greatness...





## Back to the "small" scales: galaxy clusters

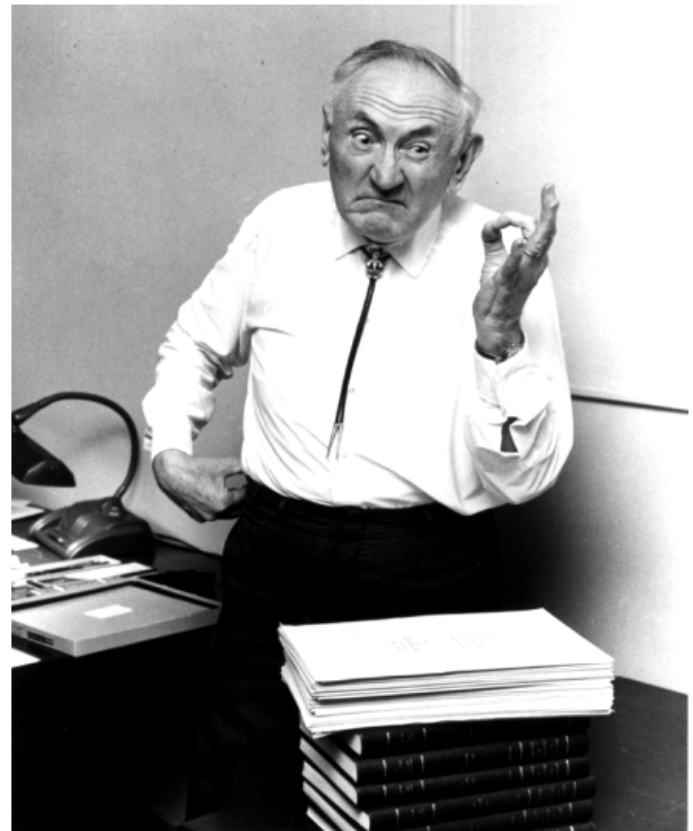
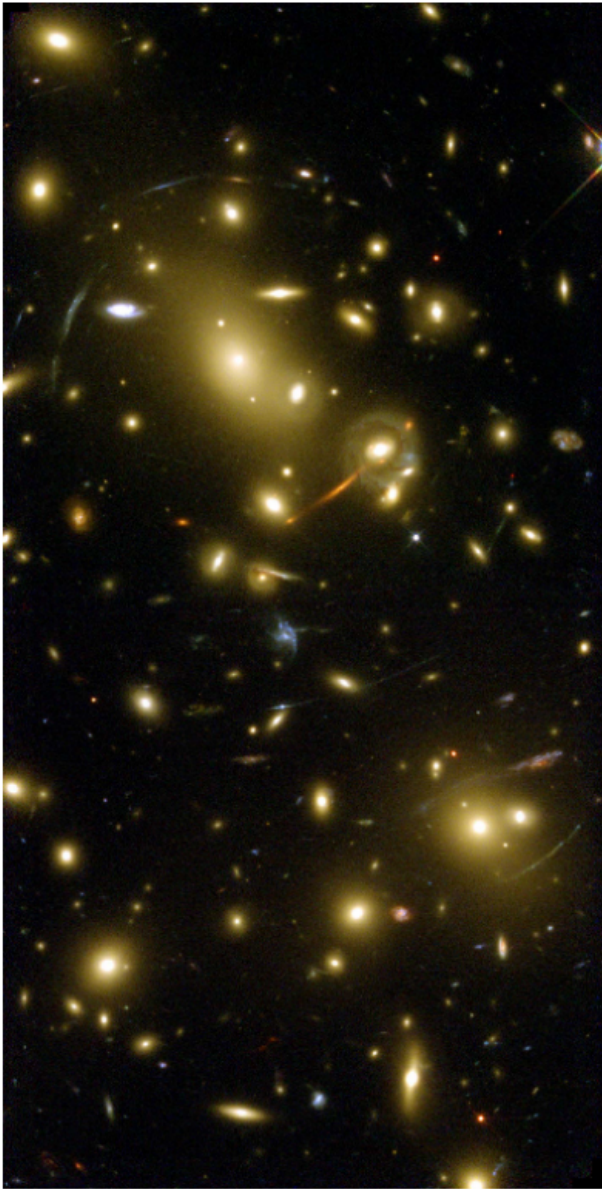


Perseus cluster:

'Constellation' of galaxies

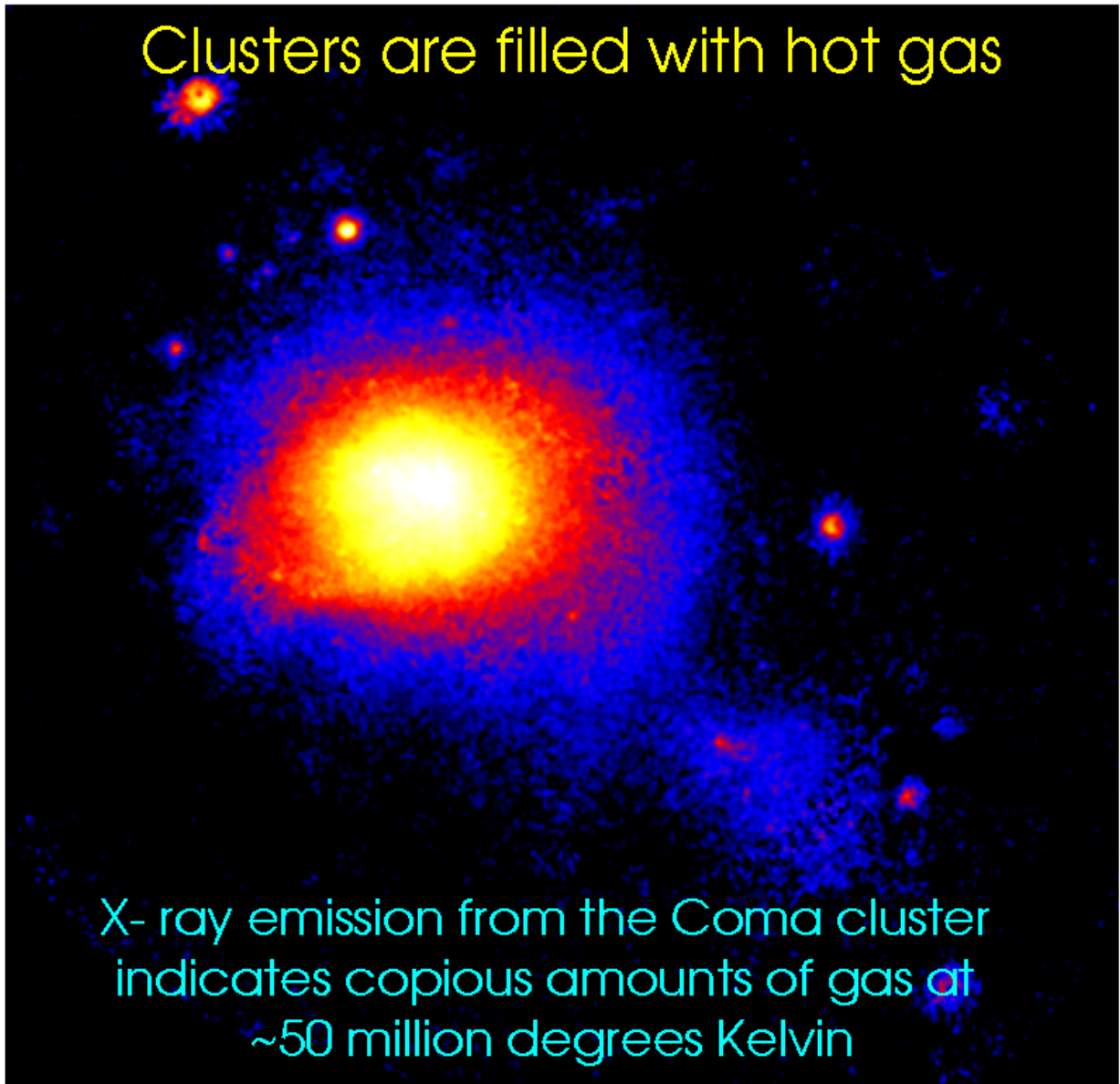


# Clusters and Dark Matter



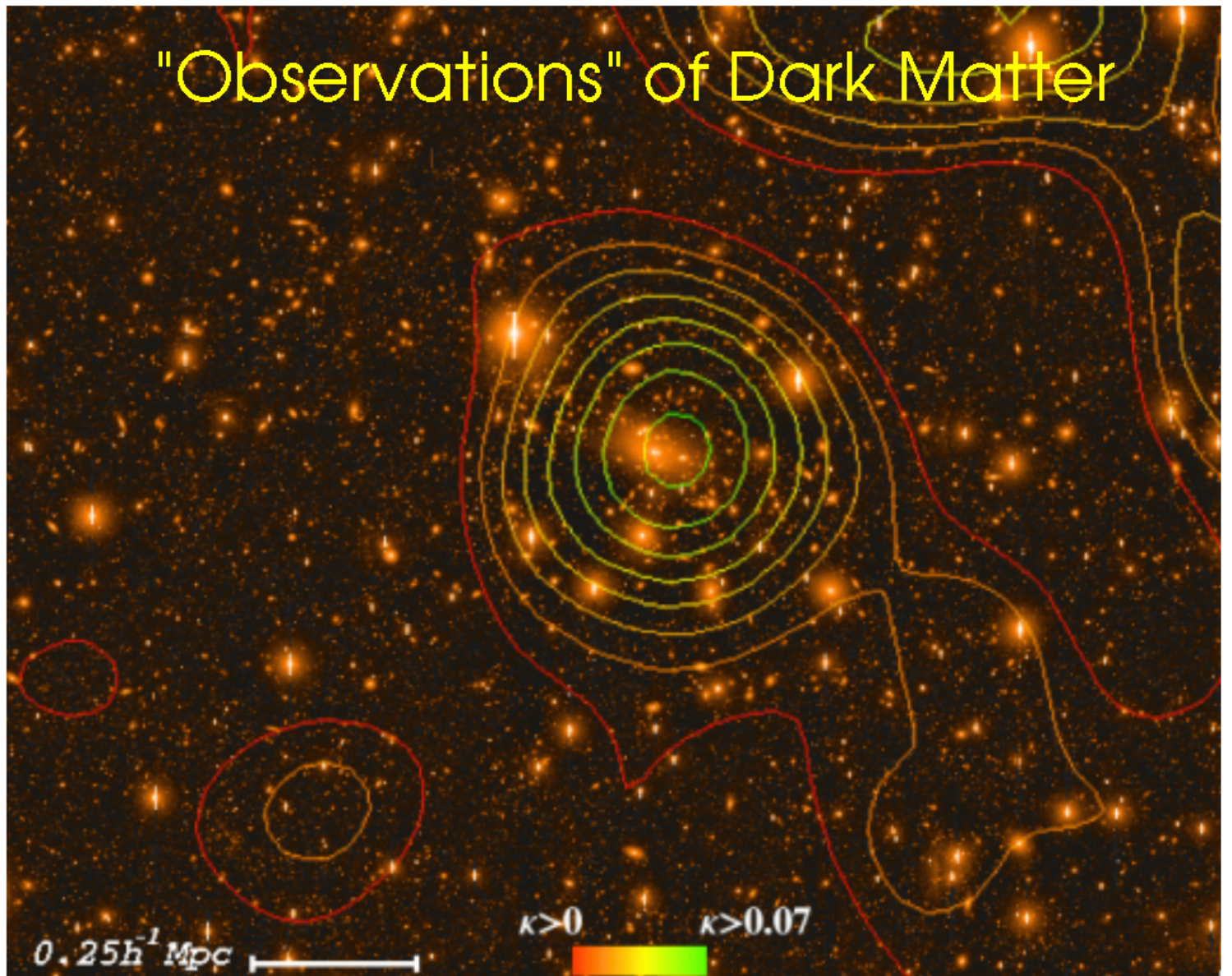
**Fritz Zwicky**  
(1898- 1978)

Clusters are filled with hot gas



X- ray emission from the Coma cluster  
indicates copious amounts of gas at  
~50 million degrees Kelvin

# "Observations" of Dark Matter



## (Some of) The Current Cosmological Mysteries

- Is the Universe full of weird dark matter? Or, even weirder, dark energy?

*the answer appears to be YES. how we know? what is Dark Matter?  
what is Dark Energy*

- How did it all begin? How did the structures form?

*understanding how the structures, and galaxies in particular, form is  
critical to understanding the origins of everything we see around us,  
including the intelligent life*

- How do we find out?

*a variety of new observations, sophisticated computer modeling using  
modern supercomputers*



## Einstein's theory of General Relativity

curvature of space = matter + energy

### Content of the Universe:

all existing components (protons, neutrons, hypothetical dark matter) contribute to gravity and can influence the rate with which the Universe expands

The contribution of each component is measured in units of

critical density:  $\Omega_i = \rho / \rho_{\text{crit}}$

$$\rho_{\text{crit}} = 3H_0^2 / 8\pi G = 1.8788 \times 10^{-29} h^2 \text{ g cm}^{-3}$$

# Content of the Universe: observational probes

## □ Ripples in the Cosmic Microwave Background

*physical processes causing tiny fluctuations in the temperature of the relic microwave radiation are well understood. we can predict them much better than the weather!*

## □ Large- scale structure of the Universe

*galaxies, galaxy clusters, filaments*

## □ Standard "candles"

*any object whose intrinsic brightness is known or can be deduced from observations without using distance. SNIa are currently the best cosmological standard candles known*

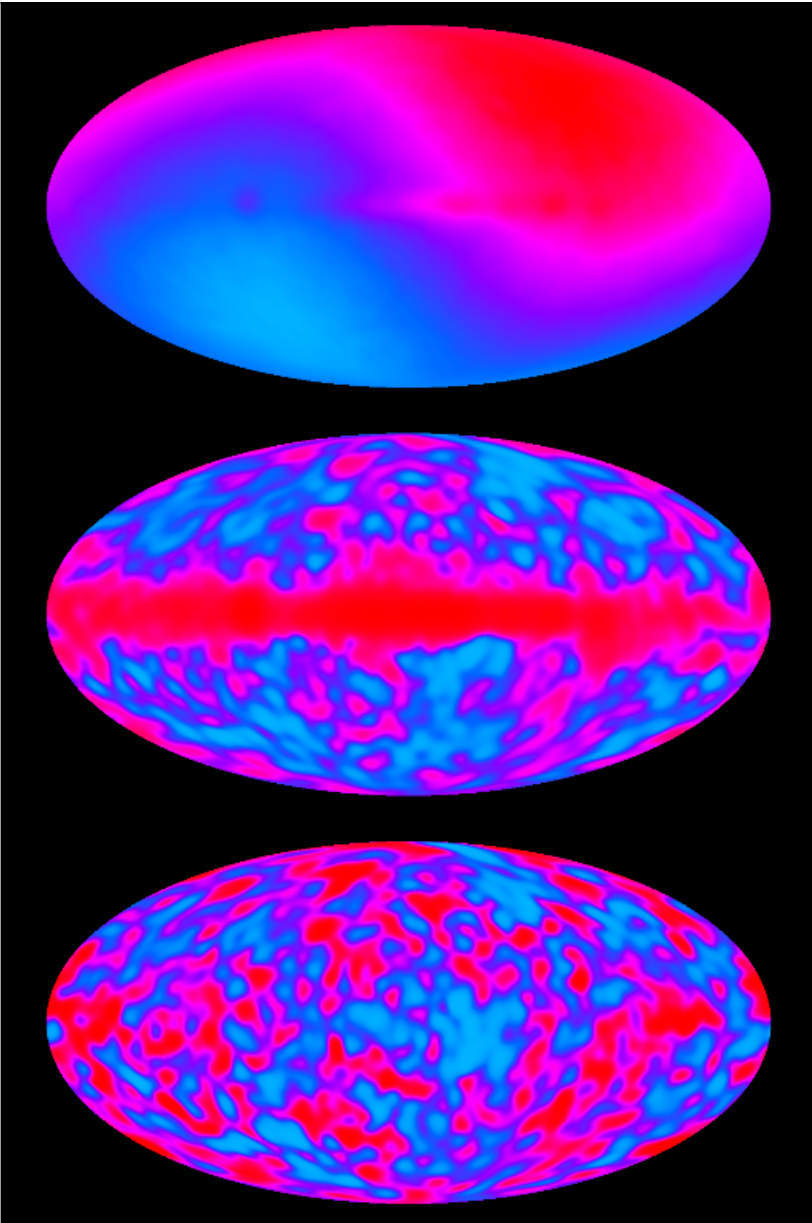
## □ Standard rulers (systems with known intrinsic size)



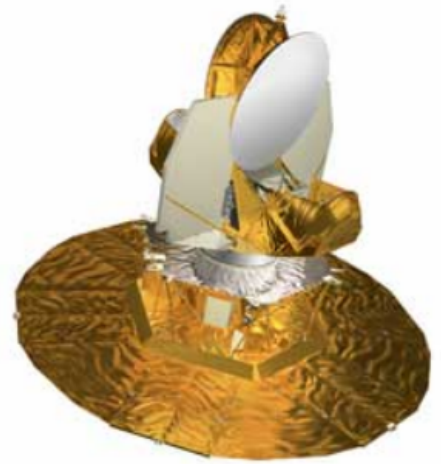
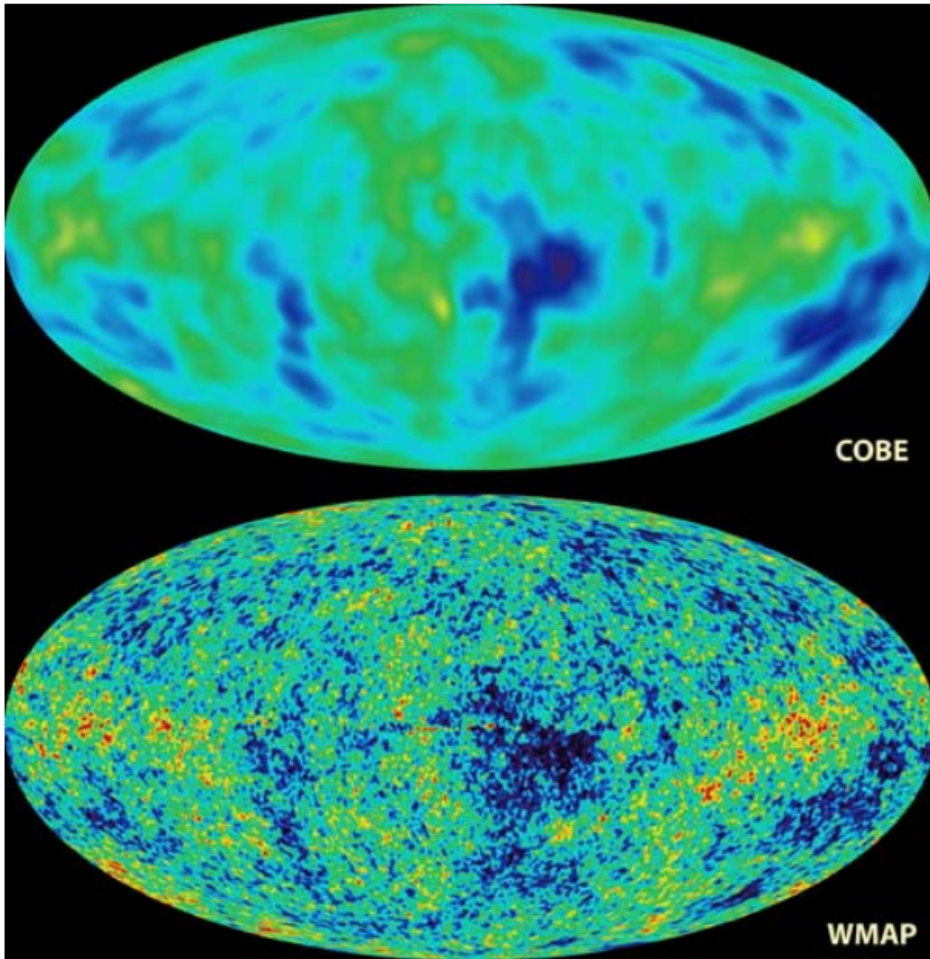
# Cosmic Microwave Background Temperature Fluctuations



COsmic Background  
Explorer (COBE)  
satellite



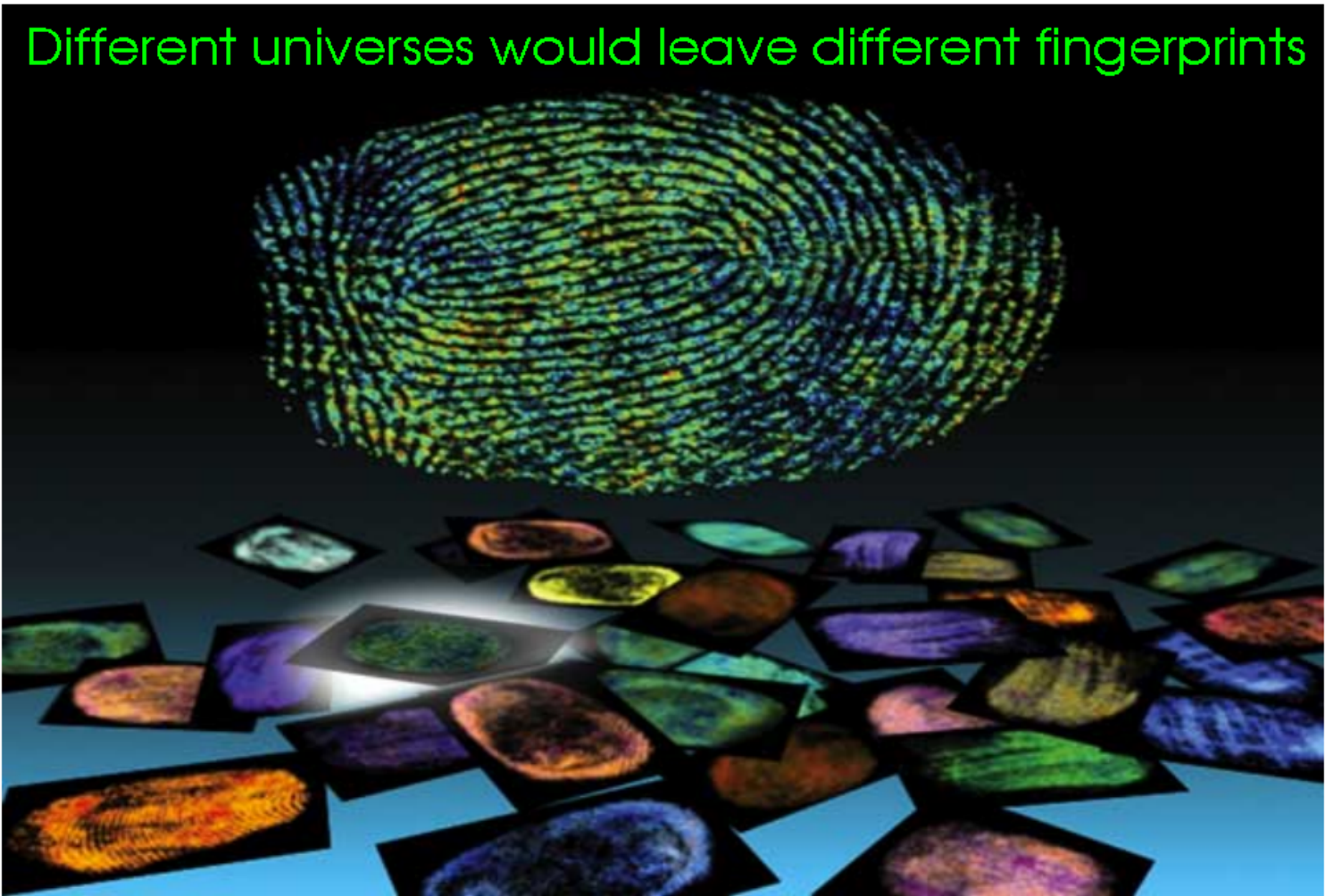
version 2003



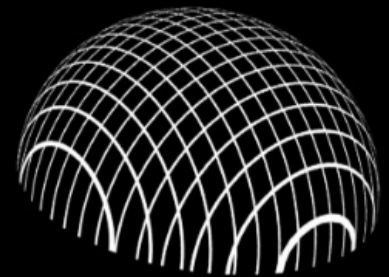
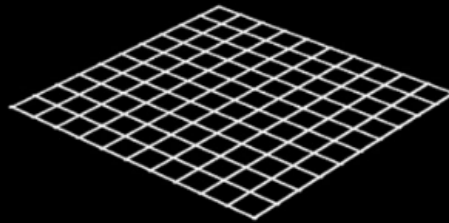
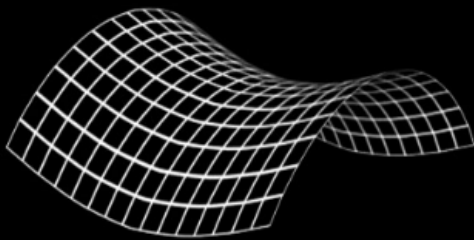
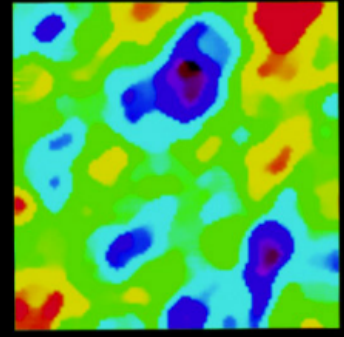
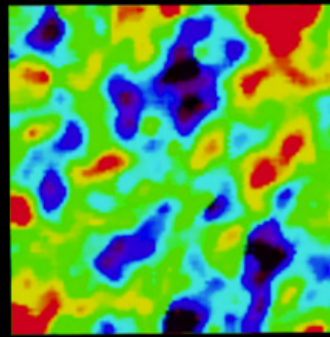
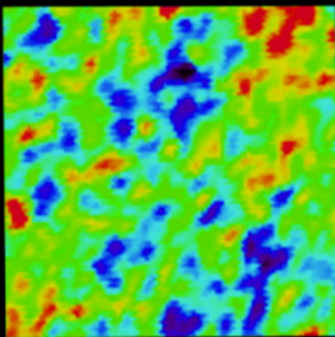
Wilkinson  
Microwave Anisotropy  
Probe  
(WMAP)  
satellite

# What do we learn?

Different universes would leave different fingerprints



# GEOMETRY OF THE UNIVERSE



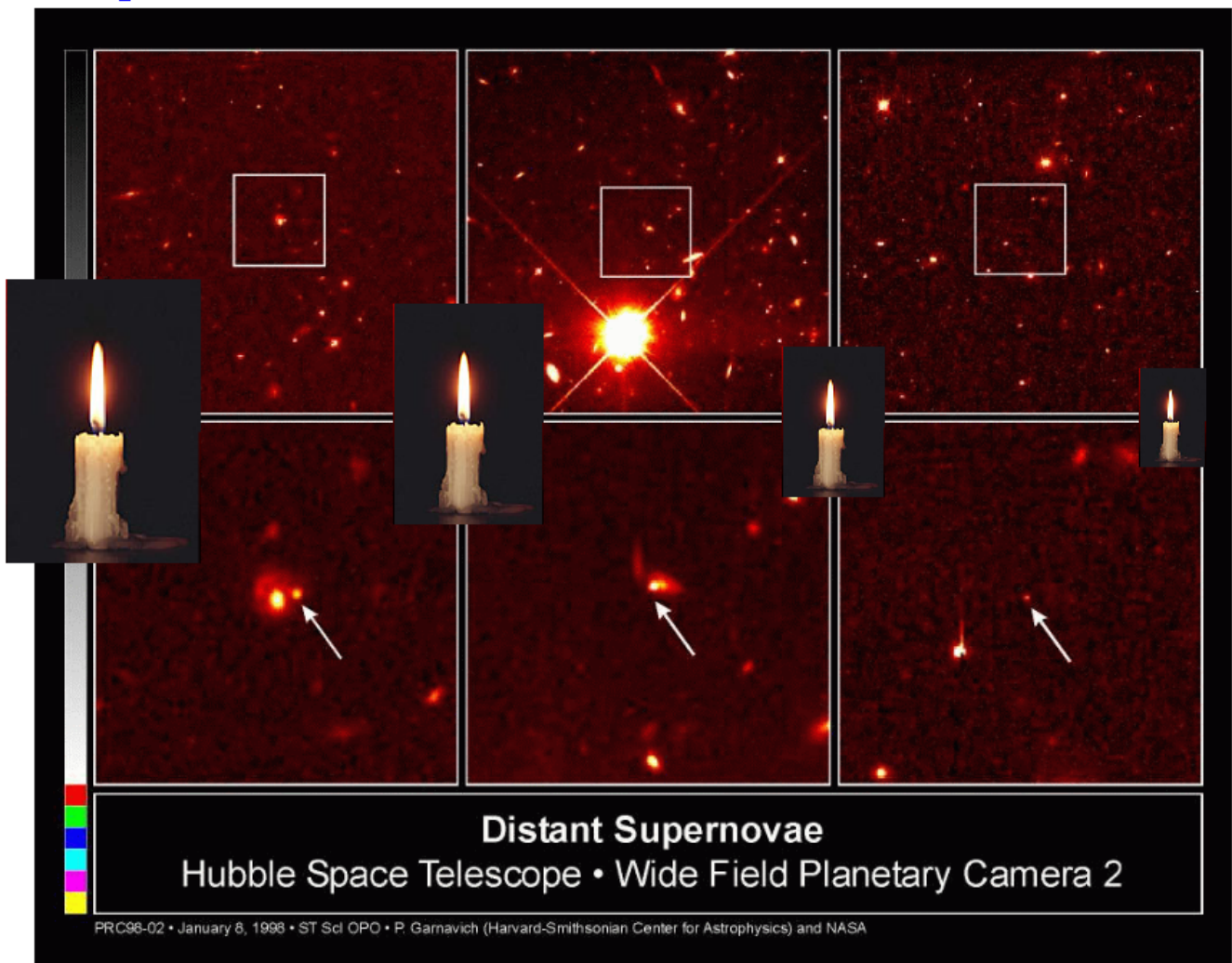
**OPEN**

**FLAT**

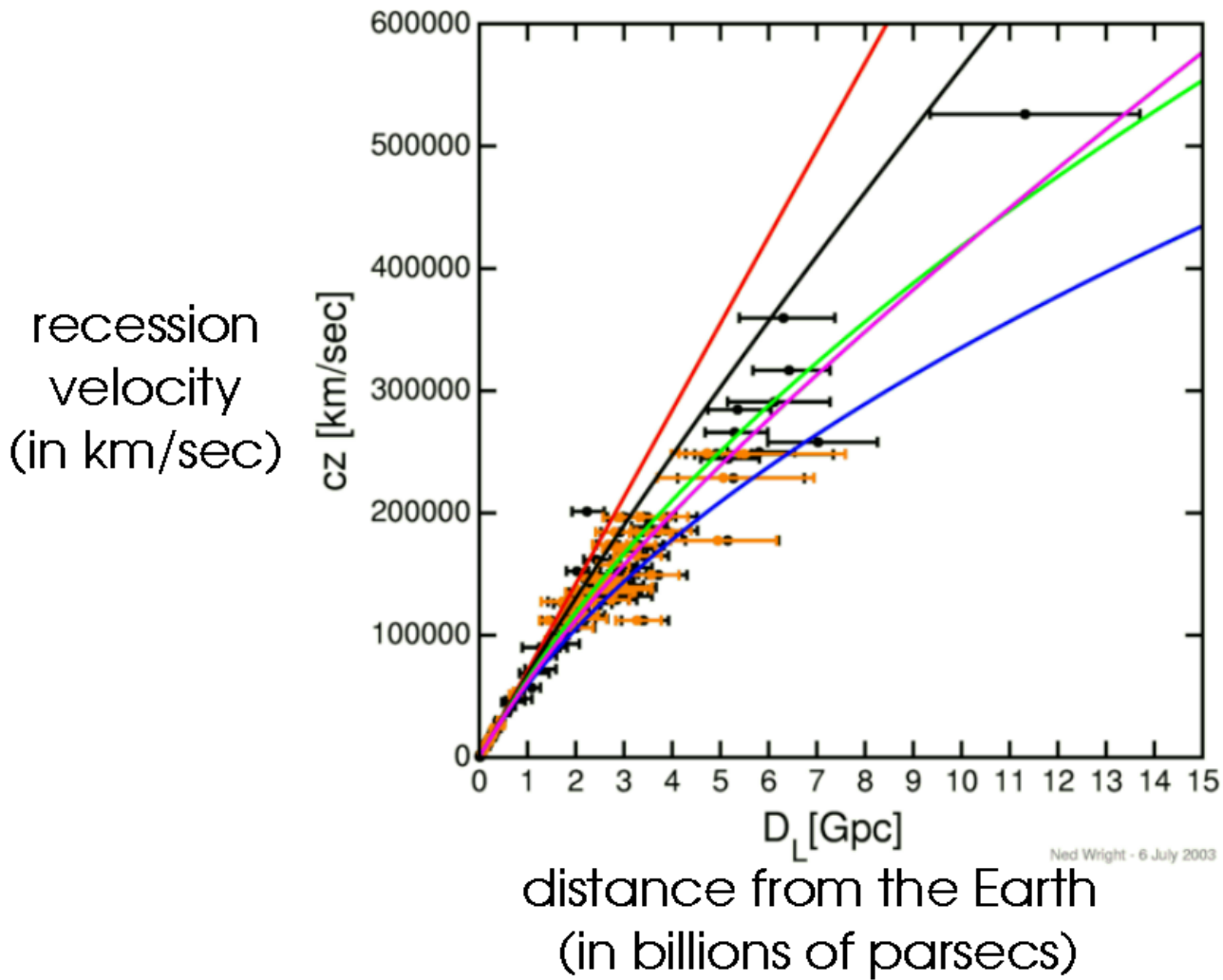
**CLOSED**

Universes with different amounts of matter would distort the CMB radiation by different amounts

# High redshift supernovae type Ia



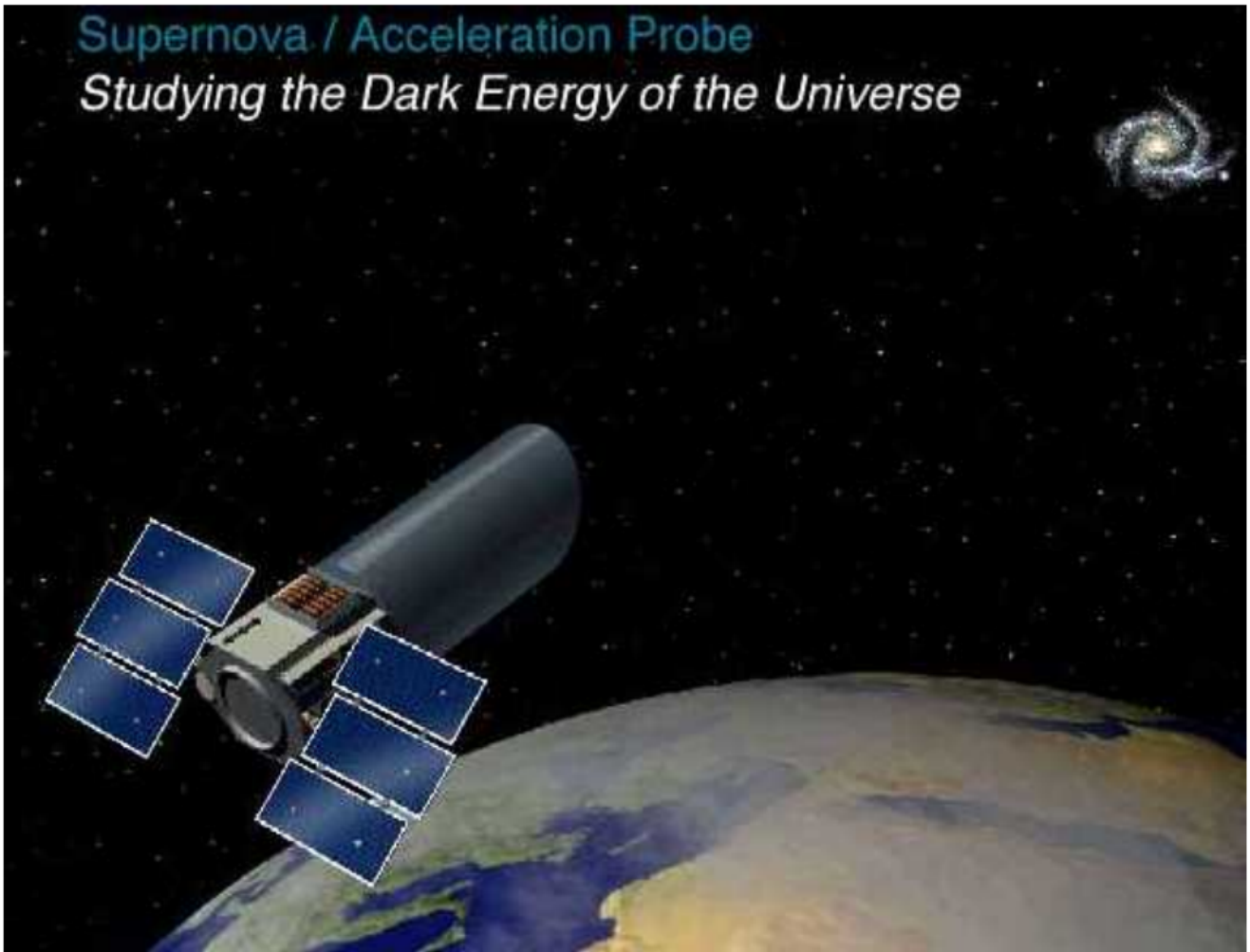
# The accelerating Universe!



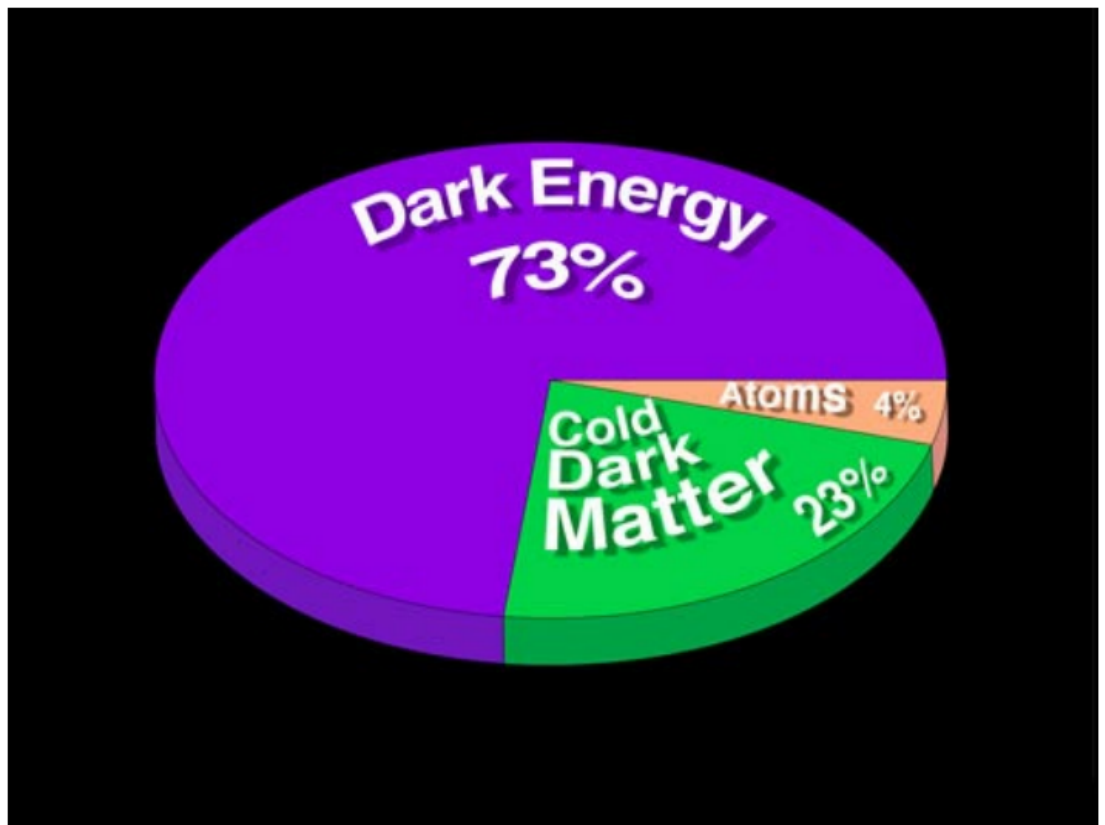
# The proposed SNAP satellite

Supernova / Acceleration Probe

*Studying the Dark Energy of the Universe*

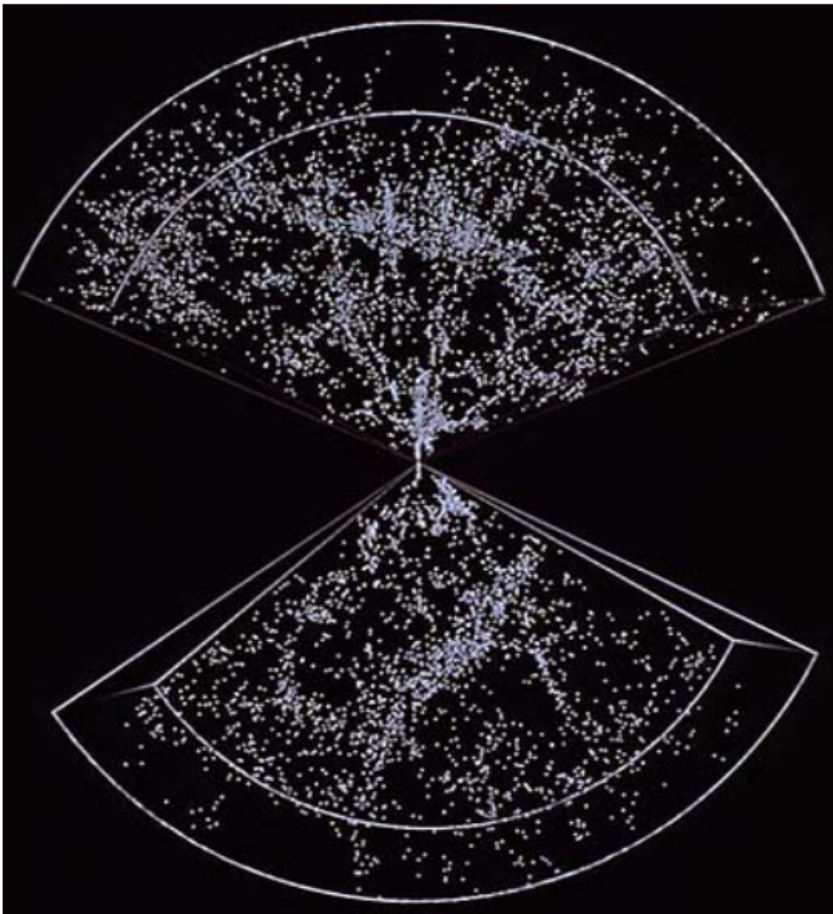


# Cosmic Pie

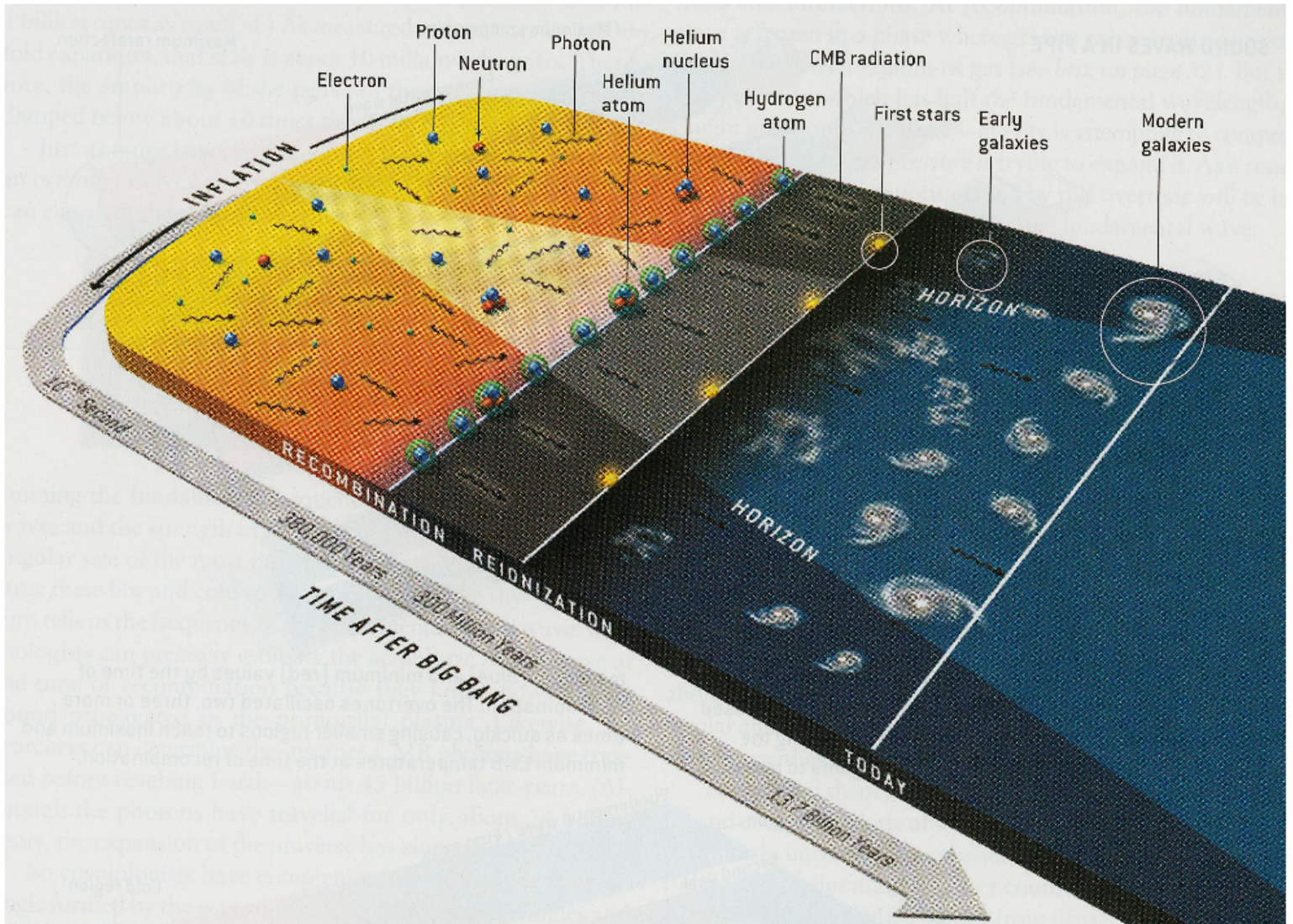




Towards a coherent picture:  
modeling structure formation in the Universe



# A Brief History of the Universe



# FORMATION OF STRUCTURES

Big Bang

$z=10^{66}$

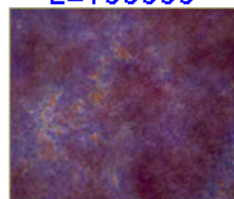


First particles form



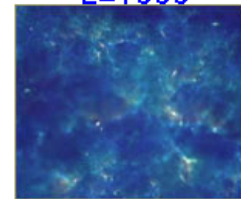
Light elements (H, He, Li) form

$z=100000$



Universe becomes neutral

$z=1000$



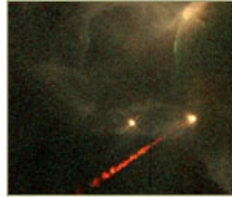
First stars form  
Universe is reionized  
 $z\sim 10$



Galaxies form  
 $z\sim 1-5$



Solar system forms  
 $z\sim 0.4$



Present day

$z=0$



# Computer Simulations: How to set up and where to begin?

- If the content of the Universe is assumed, theory predicts the statistical properties of inhomogeneities in matter distribution

*these predictions are used to set up initial conditions of the simulations*

- Simple analytic predictions are accurate only while inhomogeneities are small (<10% fluctuations with respect to the mean density of the Universe)

*simulations are initialized at an epoch before analytic predictions break down, during the so-called "Dark Ages"*

- Numerical simulations are used to follow formation of structures and make accurate predictions at later epochs where analytic calculations break down

# Computer Simulations: How do we model?

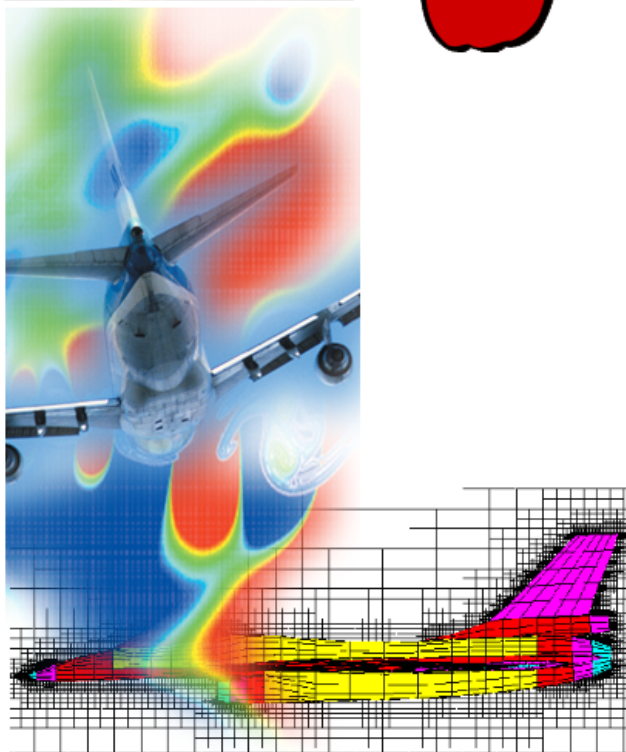


- Gravity is the king

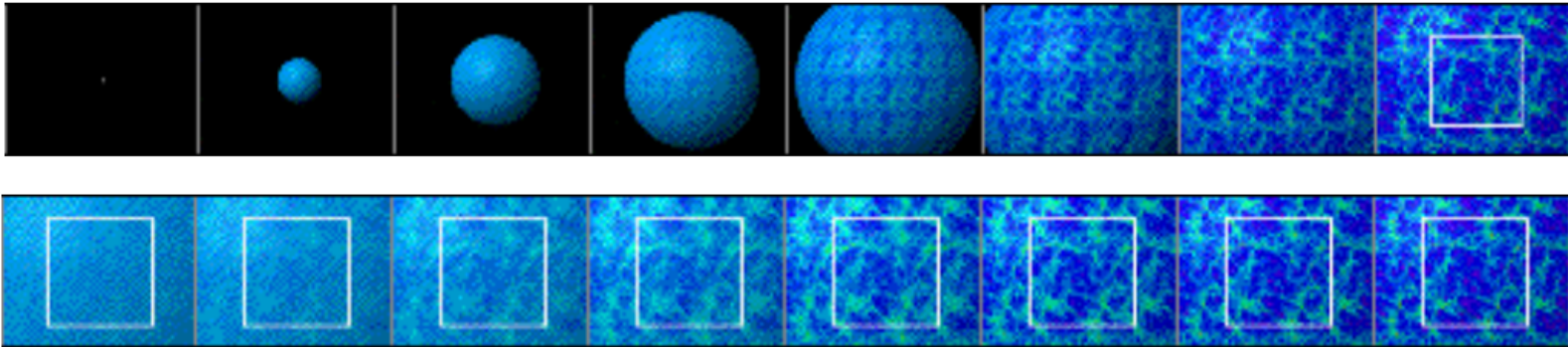
*gravity is by far the strongest force on the large scales. gravitational interactions are modelled using Newton's laws*

- Other forces may need to be included depending on the composition of the Universe and scales considered

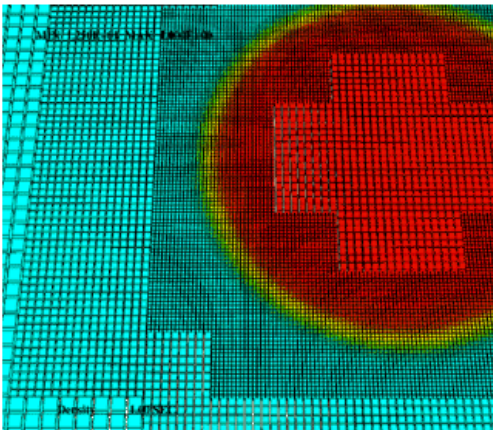
*ordinary matter, the baryons, experiences pressure forces if compressed to sufficiently high densities. these "hydrodynamic" forces are included in simulations that include baryons*



We all live in



# Computer Simulations: discretizing matter and space



- Space and time are continuous on macroscopic scales, but computers can only deal with discrete numbers
- Memory and CPU speed limit the number of volume elements and particles that we can simulate

*in the standard theories,  $10^{51} - 10^{82}$  dark matter particles are expected in a cubic Megaparsec*

*current computers can handle only up to a billion particles*

***----- > need to discretize***



# Hardware

*Supercomputers at National Centers and Labs  
(e.g., the National Center for Supercomputer Applications - NCSA)*

[www.ncsa.uiuc.edu](http://www.ncsa.uiuc.edu)



*Lots and lots of storage...*





# Many Many Lines of Software

```

-----
subroutine Split ( Level , mtot )
-----
purpose: splits cells marked to split

input  : Level - level to process
output : mtot  - # of cells just split

# include "a_def.h"
include 'a_tree.h'
include 'a_control.h'

integer mtot, Level
integer idcell
real*8 e_kin, e_ip
real*8 whvar(nhvar), wvar1, wvar2, wvar3
dimension iPyr(nchild,3) ! interpolation pyramid vertices

data iPyr / 1, 2, 1, 2, 1, 2, 1, 2,
&          3, 3, 4, 4, 3, 3, 4, 4,
&          5, 5, 5, 5, 6, 6, 6, 6 /

c.... Warning! The loops below are to be executed SERIALLY
c
IF ( Level .eq. MinLevel ) THEN
  do icl = 1 , ncell0
    if ( vvw(1,icl) .gt. wsplit ) then
      ires = iSplitCell ( icl )
      if ( ires .eq. nil ) then
        mtot = mtot + 1
        i0c = i0ct0h(icl)
        v_p = hvar(3,icl)**2 +
&          hvar(4,icl)**2 +
&          hvar(5,icl)**2

```

```

else
  if ( sta(1) .gt. eps ) then
    xcl = ( al + p_1 + bl ) / ( p_1 + cl )
    w2l = 1./sqrt(max(small_R, xcl**2 + stl(1)**2 + (p_1 + stl(3))**2))
    u1l = stl(2) + ( stl(3) - p_1 ) * w2l
    xxr = ( ar * p_1 + br ) / ( p_1 + cr )
    w2r = 1./sqrt(max(small_R, xxr**2 + str(1)**2 + (p_1 + str(3))**2))
    ur1 = str(2) + ( p_1 - str(3) ) * w2r
    p2 = max ( small_R , 1.0000001 * p_1 - ( ur1 - u1l )
              * abs( p_1 - p_0 )
              / ( abs( ur1 - ur_0 )
                + abs( u1l - ul_0 )
                + small_R ) )
    p_0 = p_1
    p_1 = p2
    ul_0 = u1l
    ur_0 = ur1
    devi = abs ( p2 - p_1 ) / ( p2 + p_1 )
    sta(1) = devi
    dev = max ( dev , devi )
  endif
endif
iter = iter + 1
if ( iter .le. maxit .and. dev .gt. eps ) go to 1

Bad news !!!

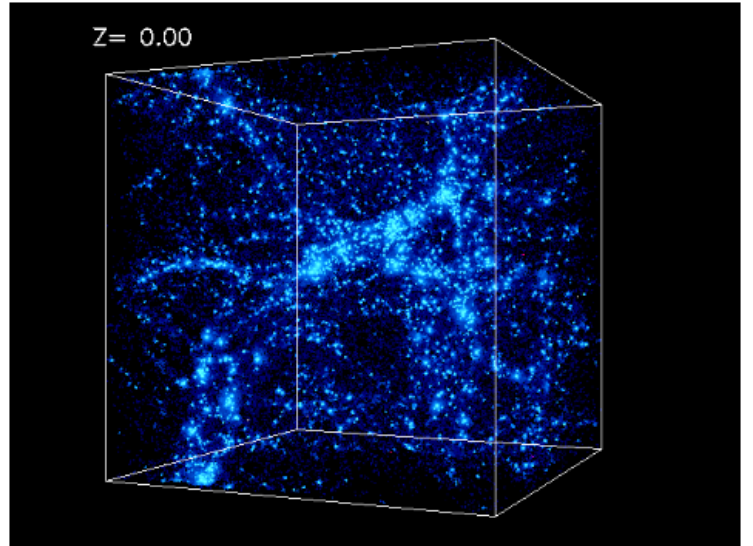
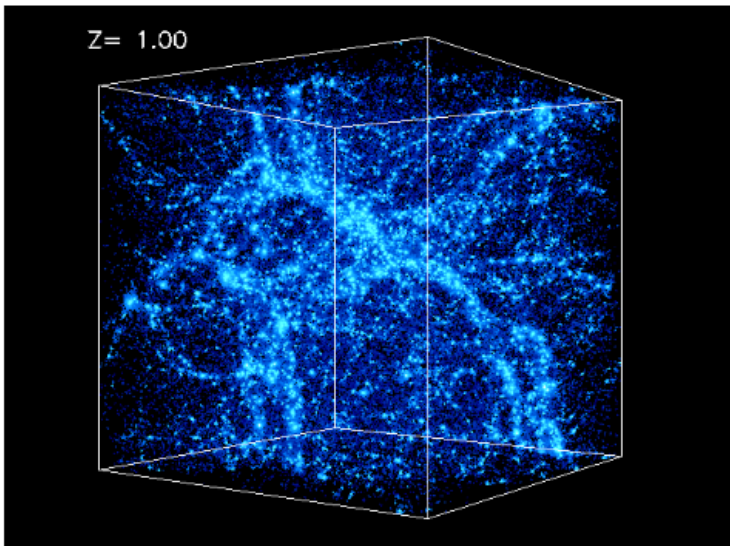
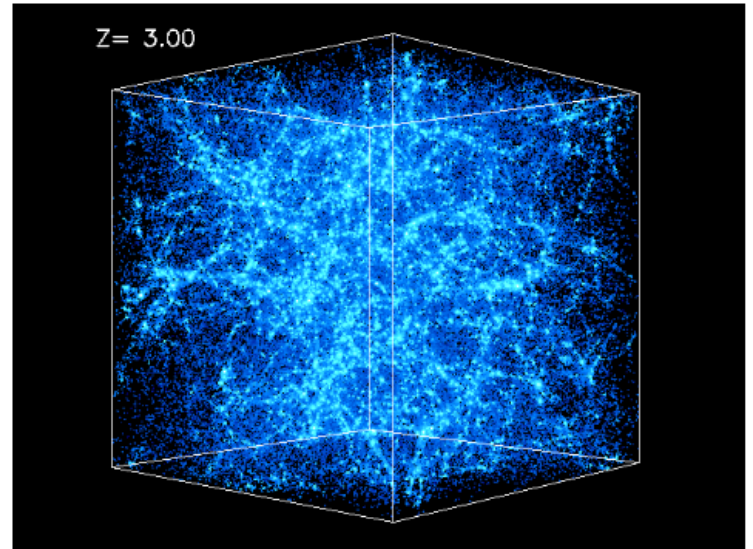
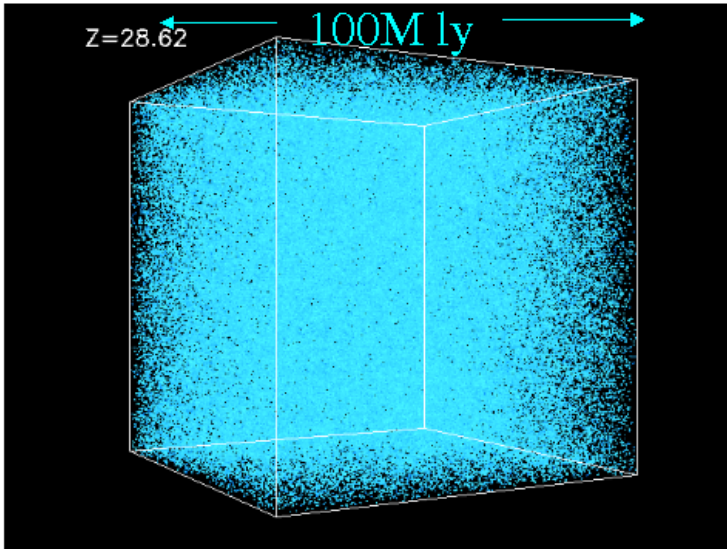
if ( dev .gt. eps ) then
  write(*, '(lx, "Riemann_1 solver iteration failure" )' )
  stop
endif

State at x/t=0

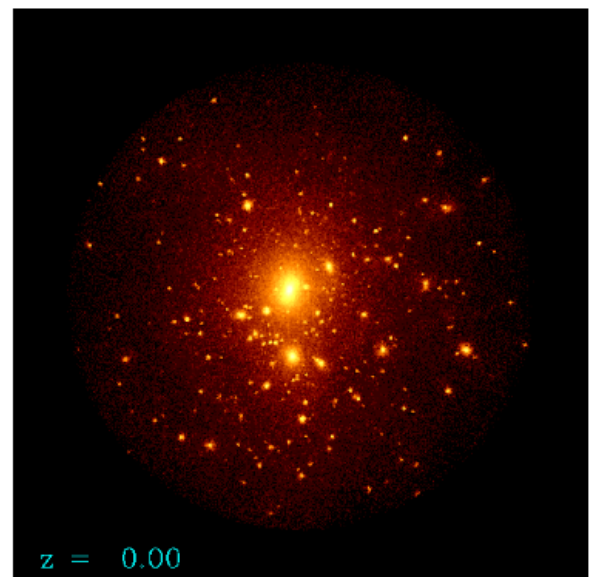
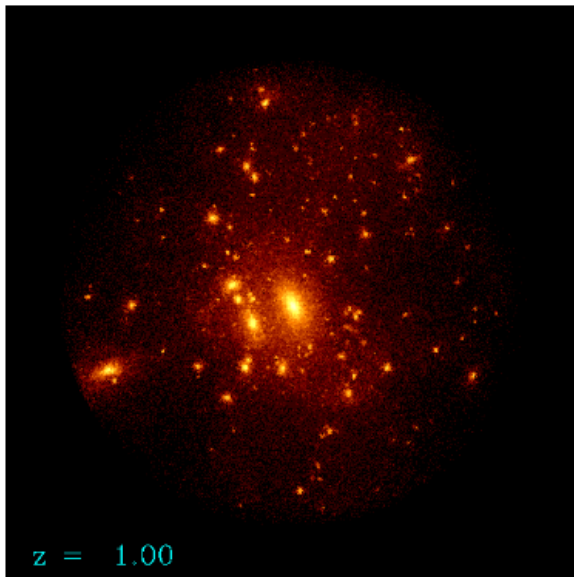
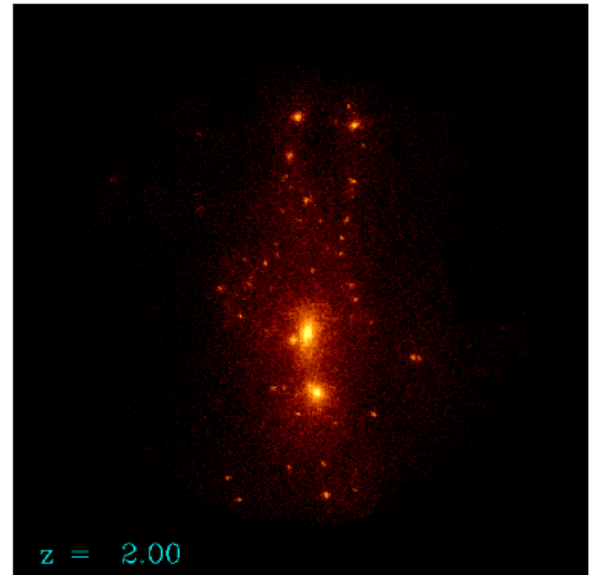
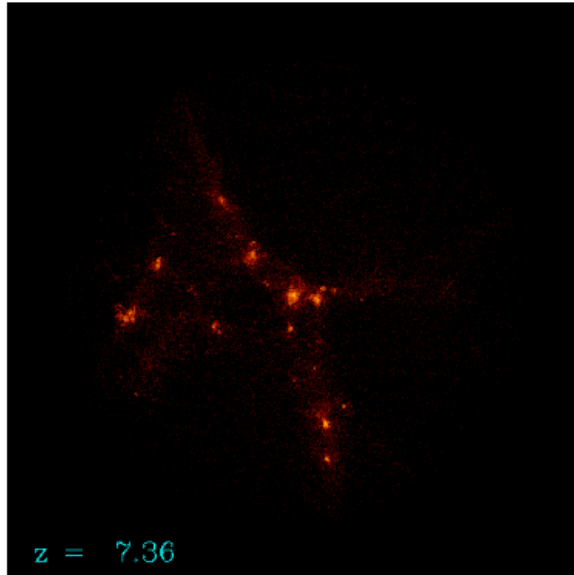
u      = 0.5 * ( ul_0 + ur_0 )
ind_r  = int ( 0.9 - sign ( onehalf , u ) )
rho_s  = ind_r * (str(1) - stl(1)) + stl(1)
u_s    = ind_r * (str(2) - stl(2)) + stl(2)
p_s    = ind_r * (str(3) - stl(3)) + stl(3)
bgam_s = ind_r * (str(4) - stl(4)) + stl(4)
qam_s  = ind_r * (str(5) - stl(5)) + stl(5)

```

## Universe in a box: formation of a filament



modeling  
formation  
of a galaxy  
cluster



10 million  
light years



## Towards simulating realistic galaxies



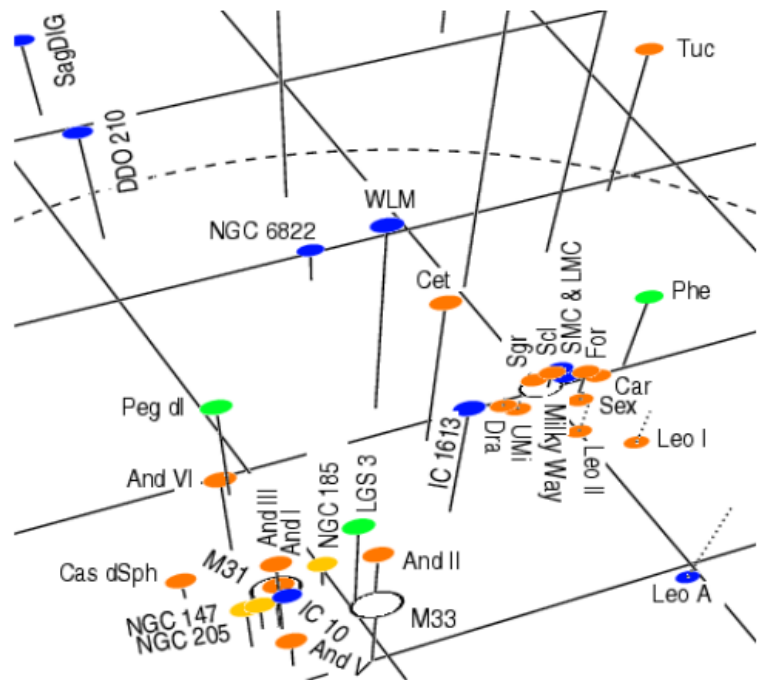
A cluster or a galaxy?



# Modeling the Local Group

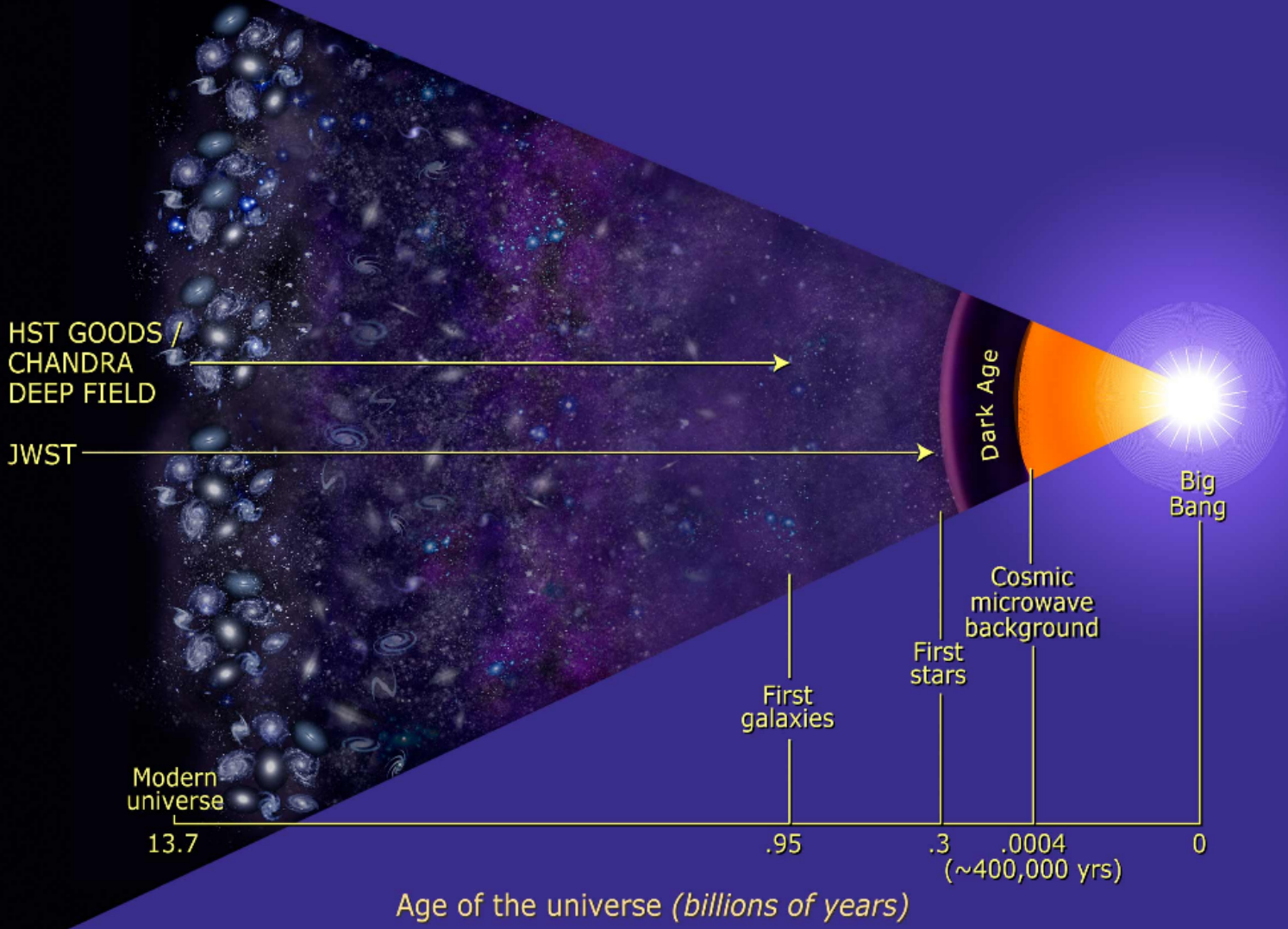


computer simulation



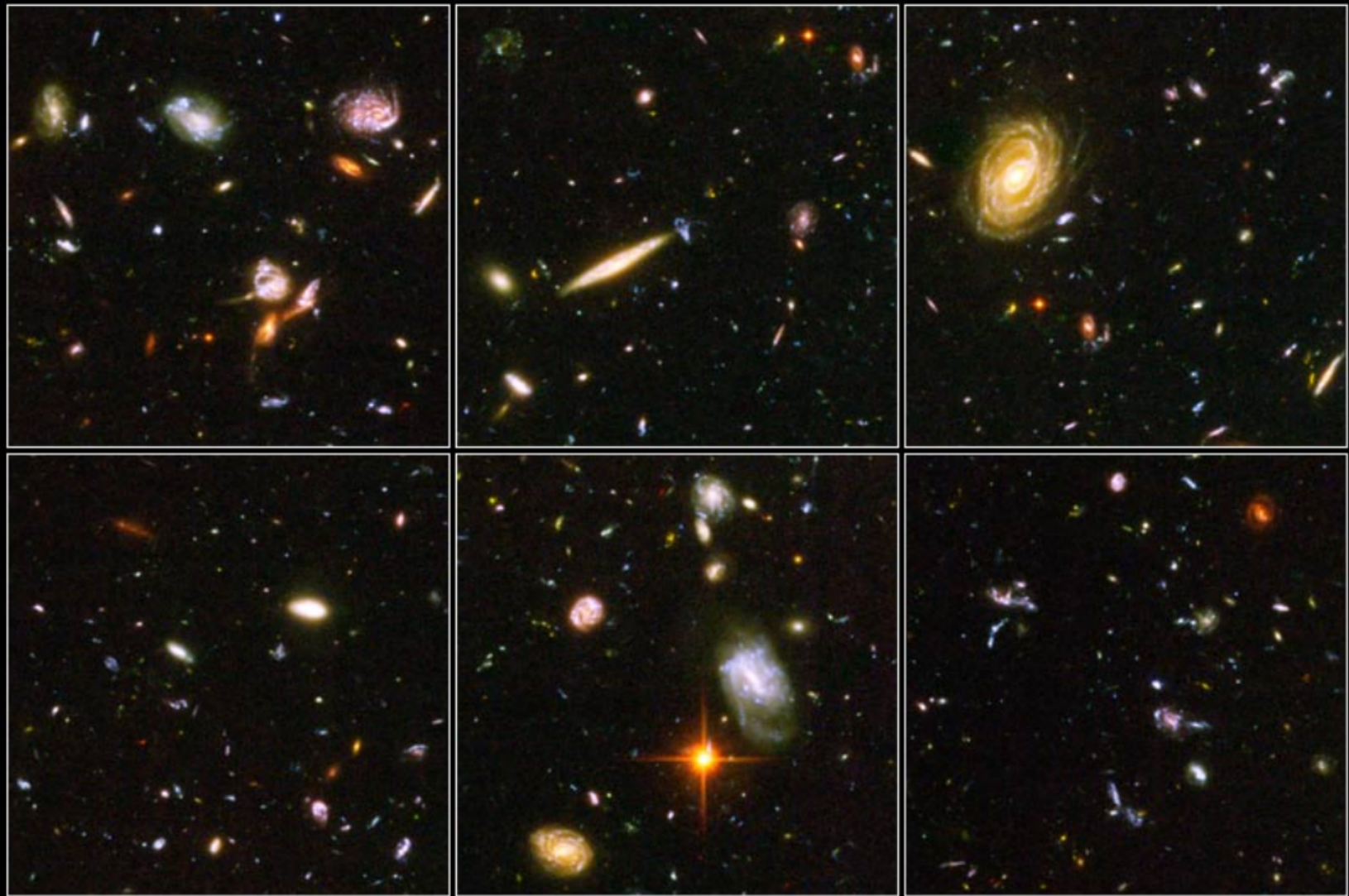
The Local Group

# Seeing back into the cosmos



Hubble Ultra Deep Field Details

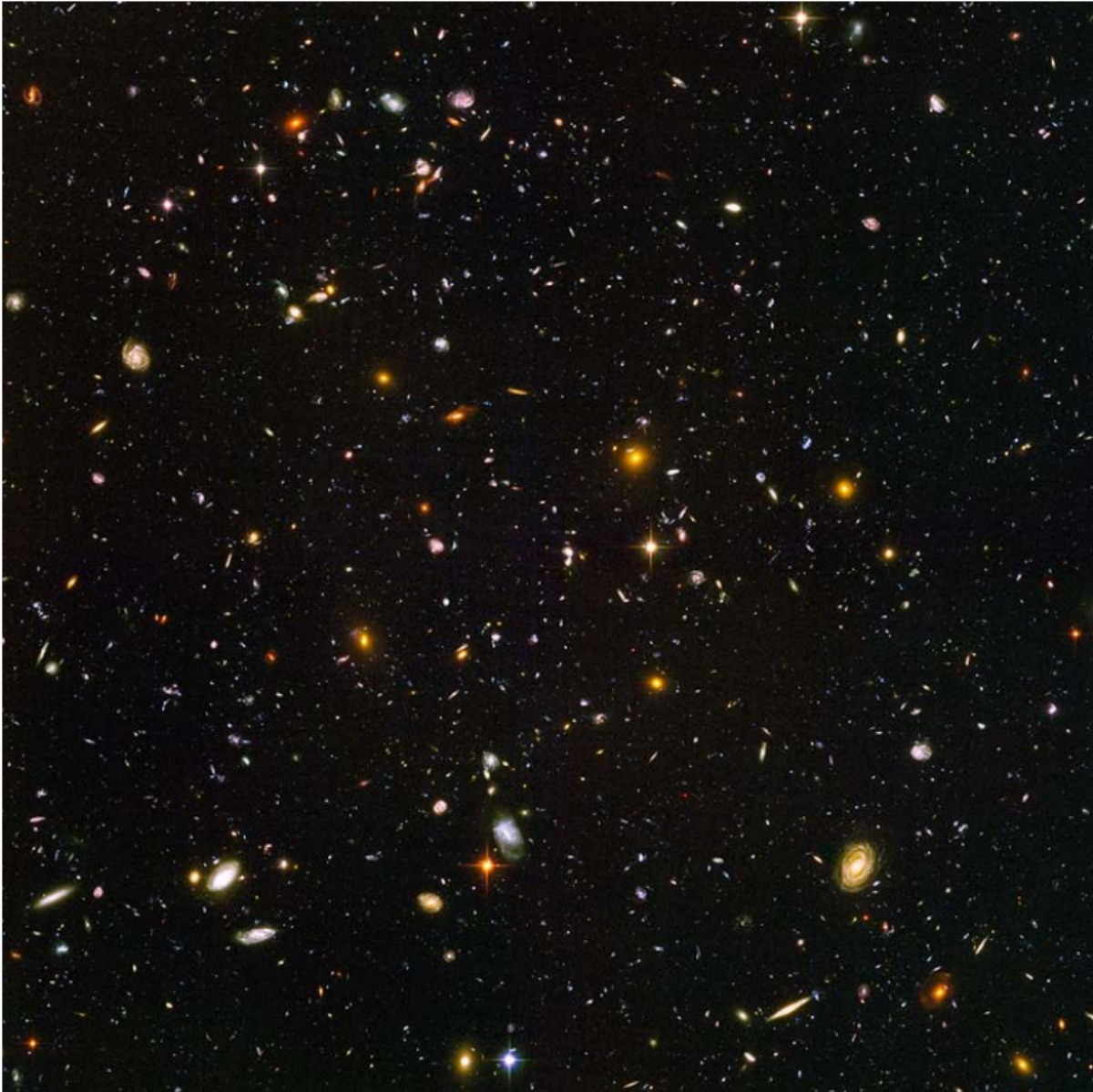
HST ■ ACS



NASA, ESA, S. Beckwith (STScI) and The HUDF Team

STScI-PRC04-07c







# Additional Reading

Slides of this talk:

<http://astro.uchicago.edu/~andrey/talks/mysteries>

Animations:

<http://efcp.uchicago.edu/lss>

Scientific American, February 2004

[The Elegant Universe](#) by Brian Greene, Norton, 2003

[The Extravagant Universe](#) by Robert Kirshner, 2002

[Voyage to the Great Attractor](#) by Alan Dressler, 1994

Map of the Universe:

[www.astro.princeton.edu/~mjuric/universe](http://www.astro.princeton.edu/~mjuric/universe)

Wilkinson Microwave Anisotropy Probe:

[map.gsfc.nasa.gov](http://map.gsfc.nasa.gov)